



LABORATORIO DI VISIONE ARTIFICIALE

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Tecniche e Strumenti per l'Elaborazione di Immagini
ed il Riconoscimento di Forme

Parte II: Livello Alto e Strumenti Disponibili

8.

27 Novembre 1989

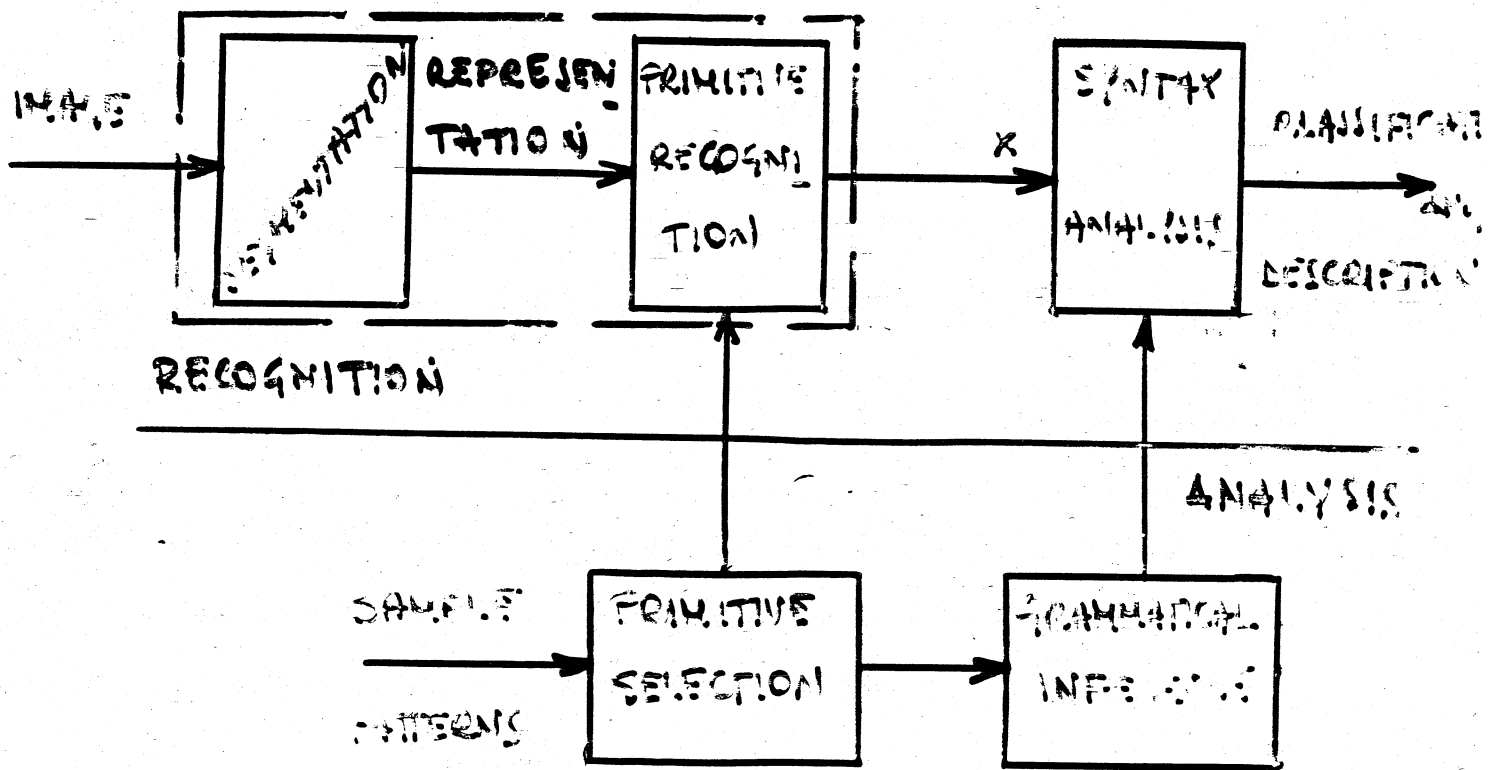
c/o SPERONI Spa, Spessa Po

V. Cantoni:

*Riconoscimento di Forme:
Approccio Sintattico-Linguistico ed
Approccio Strutturale.*

Dipartimento di Informatica e Sistemistica, Università degli Studi di Pavia

BLOCK DIAGRAM OF LINEAR SHAPE RECOGNITION



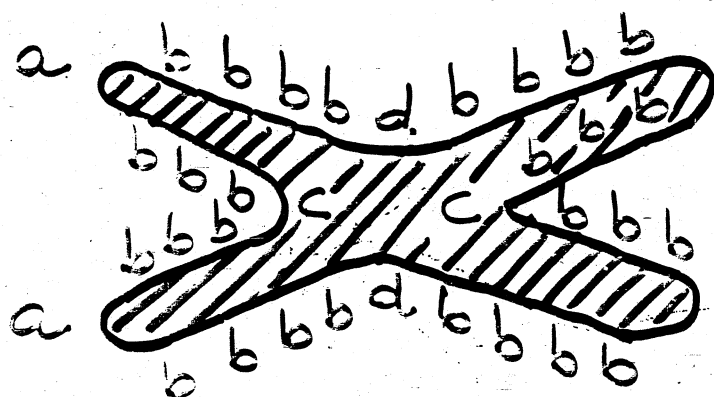
SYNTAX ANALYSIS : F.F.M.VAR: CONSIDERATIONS!

- THERE ARE APPLICATIONS IN WHICH THE STRUCTURE OF A SHAPE PLAYS AN IMPORTANT ROLE IN CLASSIFICATION PROCESS. THE SYNTACTIC APPROACH TO SHAPE RECOGNITION POSSESSES THE STRUCTURE HANDLING CAPABILITY REQUIRED. IT IS BASED ON CONCEPTS FROM FORMAL LANGUAGE THEORY.
- BASIC TO THE SYNTACTIC SHAPE RECOGNITION APPROACH IS THE DECOMPOSITION OF SHAPE INTO SUBPATTERNS OR PRIMITIVES
- EACH PRIMITIVE IS USED AS A POSSIBLE SYMBOL OF A GRAMMAR, WHERE A GRAMMAR IS A SET OF RULES OF SYNTAX FOR THE GENERATION OF SENTENCES FROM THE GIVEN SYMBOLS
- GIVEN A SENTENCE REPRESENTING AN INPUT SHAPE THE PROBLEM IS THAT OF DECIDING IN WHICH LANGUAGE (WHICH GRAMMAR) THE SENTENCE IS VALID

$$G = (V_n, V_t, P, \Sigma)$$

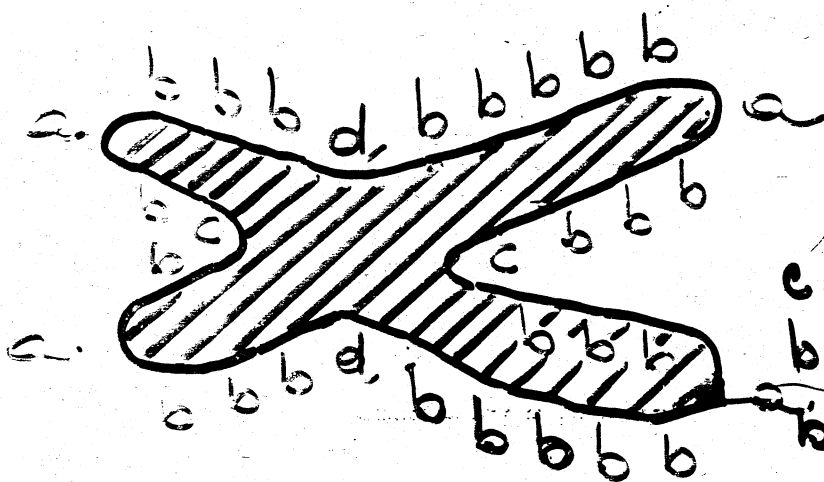
V_n : non-terminal symbols
 V_t : terminal symbols
 P : production rules
 Σ : alphabet

CHROMOSOME CLASSIFICATION



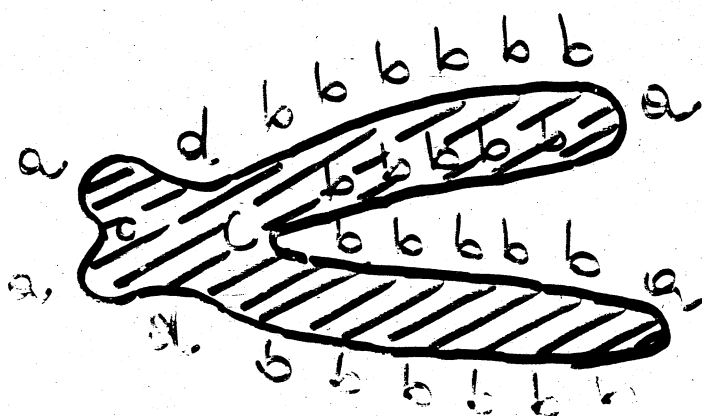
MEDIAN

c b b b a b b b d b b b
a b b b c b b b a b b b
b b b b a b b b



SUBMEDIAN

c b a b b b d b b b b
b b b c b b b a b b b b
b c



ACROCENTRIC

e a d b b b b b a b b b
b e b b b b a b b b b
d a

LINGUISTIC APPROACH TO CHROMOSOME CLASSIFICATION

THREE CONTEXT-FREE GRAMMARS HAVE BEEN DEVELOPED, EACH DESCRIBING ONE CLASS OF CHROMOSOME: MEDIAN SUBMEDIAN ACROCENTRIC.

TERMINAL SET: V_T

$\uparrow (a \quad b \rightarrow \quad c \quad d)$

MEDIAN:

P:	$S \rightarrow AA$	$A \rightarrow cB$	$B \rightarrow FBE$	$B \rightarrow HDJ$
	$D \rightarrow FDE$	$D \rightarrow d$	$F \rightarrow b$	$E \rightarrow b$
	$H \rightarrow a$	$T \rightarrow a$		

SUBMEDIAN:

P:	$S \rightarrow AA$	$A \rightarrow cM$	$B \rightarrow FBE$	$B \rightarrow FL$
	$B \rightarrow RE$	$D \rightarrow FDE$	$D \rightarrow FG$	$D \rightarrow WE$
	$L \rightarrow EL$	$R \rightarrow RE$	$G \rightarrow FG$	$W \rightarrow WE$
	$F \rightarrow b$	$E \rightarrow b$	$H \rightarrow a$	$M \rightarrow FBE$
	$T \rightarrow a$	$L \rightarrow HNT$	$R \rightarrow HNT$	$G \rightarrow d$
	$W \rightarrow d$	$N \rightarrow FDE$		

ACROCENTRIC

P:	$S \rightarrow AA$	$A \rightarrow cB$	$B \rightarrow FL$	$B \rightarrow RE$
	$D \rightarrow FG$	$D \rightarrow WE$	$L \rightarrow FL$	$R \rightarrow RE$
	$G \rightarrow FG$	$W \rightarrow WE$	$L \rightarrow HDJ$	$H \rightarrow a$
	$R \rightarrow HDJ$	$G \rightarrow d$	$W \rightarrow d$	$T \rightarrow a$
	$E \rightarrow b$	$F \rightarrow b$		

ATTRIBUTED GRAMMAR.

AN ATTRIBUTED GRAMMAR IS A GRAMMAR WHERE:

- EACH PRIMITIVE OR NONTERMINAL HAS A SYMBOLIC PART AND A VALUE PART WHICH MAY HAVE SEVERAL ATTRIBUTES
 - EACH SYMBOLIC PRODUCTION RULE HAS A CORRESPONDING SET OF ATTRIBUTE RULES WHICH PRODUCE THE ATTRIBUTES RELATED TO THE PRODUCTION RULE IN PARSING
 - INTRODUCTION OF A METRIC
- AS AN EXAMPLE WE CONSIDER THE TOTAL CURVE LENGTH TO BE AN ATTRIBUTE IN THE COORDINATE CLASSIFICATION

PRODUCTION RULES:

$$\begin{array}{ll}
 S \rightarrow Q_1^1 Q_1^2 & l_{S1} \leftarrow l_{Q_1^1}; l_{S2} \leftarrow l_{Q_1^2} \\
 S \rightarrow Q_1 Q_2 & l_{S1} \leftarrow l_{Q_1}; l_{S2} \leftarrow l_{Q_2} \\
 S \rightarrow Q_1 Q_2 & l_{S1} \leftarrow l_{Q_2}; l_{S2} \leftarrow l_{Q_1}
 \end{array}$$

$$\begin{array}{ll}
 Q_1 \rightarrow DR_1 & l_{Q_1} \leftarrow l_{R_1} \\
 Q_2 \rightarrow DR_2 & l_{Q_2} \leftarrow l_{R_2}
 \end{array}$$

$$\begin{array}{ll}
 R_1 \rightarrow H_1^1 CH_1^2 & l_{R_1} \leftarrow (l_{H_1^1} + l_{H_1^2}) / 2 \\
 R_2 \rightarrow H_2 C H_2 & l_{R_2} \leftarrow 0
 \end{array}$$

$$H_1 \rightarrow B^1 A B^2 \quad l_{H_1} \leftarrow (l_{B^1} + l_{B^2}) / 2$$

$$H_2 \rightarrow A$$

$$A \rightarrow a$$

$$B \rightarrow b$$

$$C \rightarrow c$$

$$D \rightarrow d$$

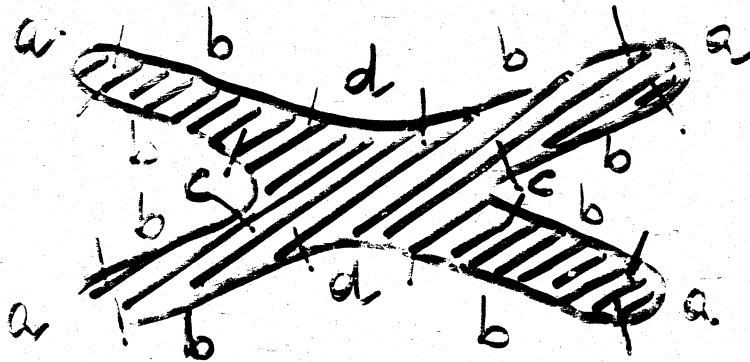
$$l_B \leftarrow :$$

Q_1 coppia
di
(R_1) propaggini
mediane o
sottomedie

Q_2 coppia di
(R_2) propaggini
eccentrici

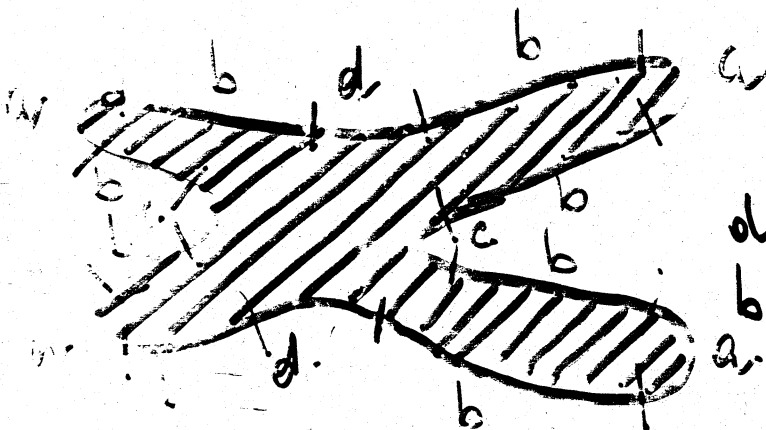
H propaggini
lingole

ATTRIBUTED GRAMMAR EXAMPLE



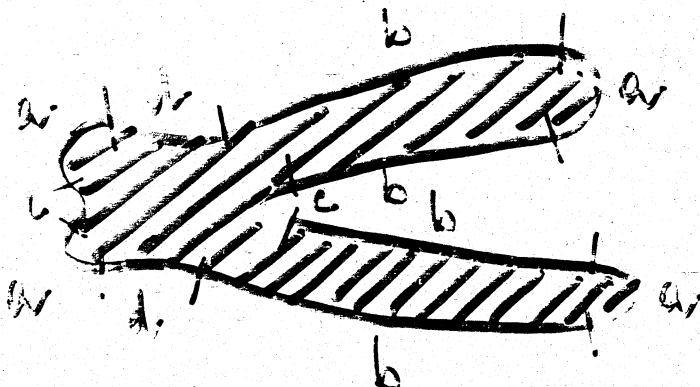
MEDIAN

$dbabcbabd$
 $babcbab$



SUBMEDIAN

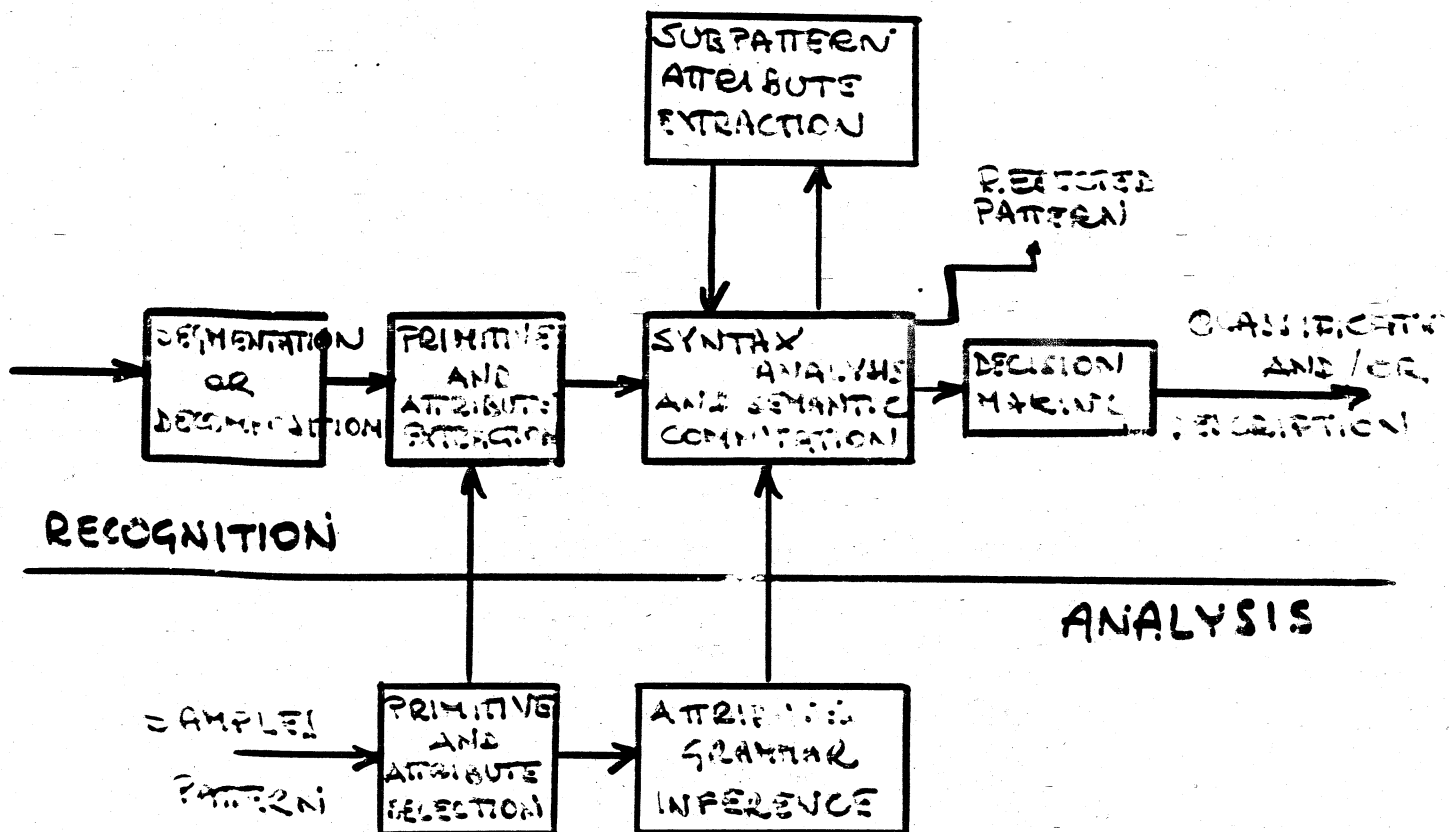
$dbabcbabd$
 $babcbab$



AROCENTRIC

$dbabcbabd$
 $acac$

SHAPE ANALYSIS SYSTEM USING ATTRIBUTED GRAMMARS

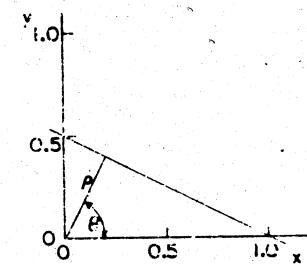


THE HOUGH TRANSFORM

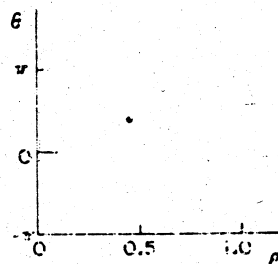
P. V. C. HOUGH : METHOD AND MEANS FOR RECOGNIZING COMPLEX PATTERNS- 1962 - U. S. PATENT 3.069.654

LINE TO POINT TRANSFORM

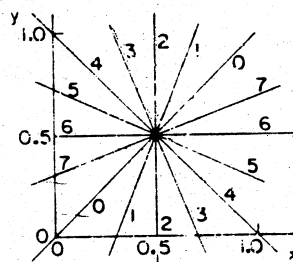
$$\rho = x \cos \theta - y \sin \theta$$



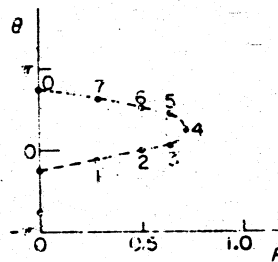
(a) PARAMETRIC LINE



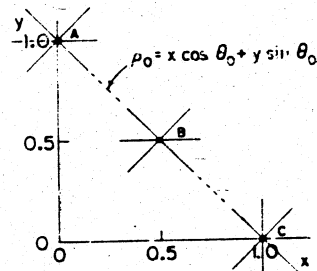
(b) HOUGH TRANSFORM OF (a)



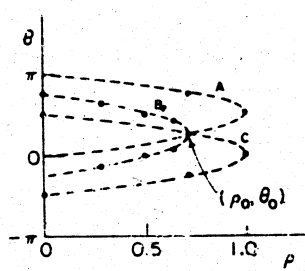
(c) FAMILY OF LINES, COMMON POINT



(d) HOUGH TRANSFORM OF (c)



(e) COLINEAR POINTS



(f) HOUGH TRANSFORM OF (e)

$$C_i = \{(x, y) \mid f(x, y, \{a_k\}) = 0\}$$

$$P = \langle a_1, \dots, a_k, i \rangle$$

$$H : C_i \rightarrow p_i \in P$$

$$H : e \in C_1 \rightarrow \Gamma(e) \subset P$$

Such that

$$\bigcap_{e \in C_1} \Gamma(e) = p_1 \in P$$

EXAMPLE

$$Z \equiv R^2 \quad i=2 \quad k=2 \quad P = \langle a_1, a_2, i \rangle$$

$$\begin{cases} y = a_1 x + a_2 x^{-1} \\ i = 1 \end{cases} \quad \begin{cases} y = a_1 x^2 + a_2 \\ i = 2 \end{cases}$$

- for each element $e \equiv (x', y')$:

$$\begin{cases} a_2 = y'x' - a_1 x'^2 \\ i = 1 \end{cases} \quad \begin{cases} a_2 = y' - a_1 x'^2 \\ i = 2 \end{cases}$$

- for each element $e \equiv (x', y', \theta)$:

$$\begin{cases} i = -1 \\ a_1 = \frac{y' + \lambda x'}{2x'} \\ a_2 = \frac{(x'y' - \lambda x')}{2} \end{cases} \quad \begin{cases} i = 2 \\ a_1 = \frac{\lambda}{2x'} \\ a_2 = y' - \frac{\lambda}{2} x' \end{cases}$$

where $\lambda = \tan \theta$

----- THE GENERALIZED HOUGH TRANSFORM -----

Let us consider a subset of points C^* which defines a model of arbitrary, non analytic shapes. We assume that all the subset of points C_i which can be produced by translating, rotating, and uniformly scaling the model C^* have the same "shape", that is belong to the family C .

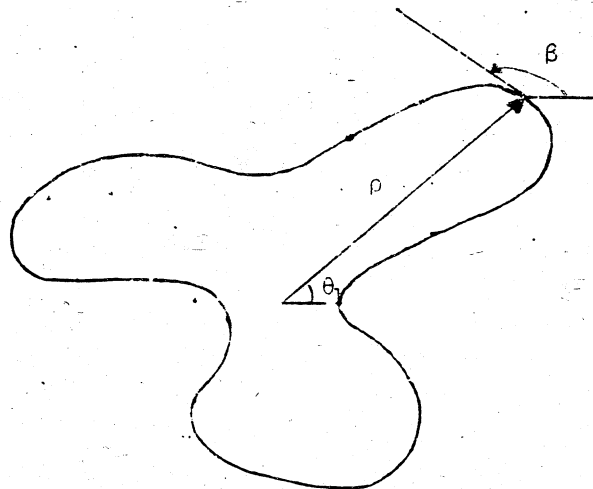
C_i is represented by a point in the four dimensional space P :

$$P = \langle x, y, \theta, s \rangle$$

where:

x, y measure the translation, θ the rotation, and s is the scaling factor.

----- MODEL DESCRIPTION -----



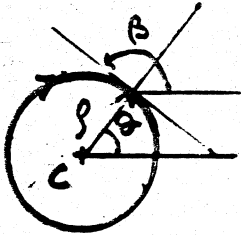
MODEL

R TABLE

θ_1	ρ_1	$\beta_1 - \theta_1$
θ_2	ρ_2	$\beta_2 - \theta_2$
θ_3	ρ_3	$\beta_3 - \theta_3$
.	.	.
.	.	.
.	.	.

EXAMPLE

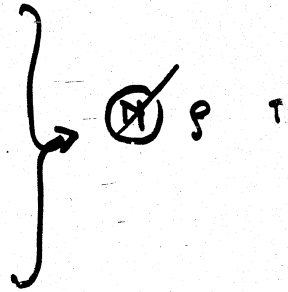
MODEL



C = REFERENCE POINTS

R-TABLE

?	$\pi/2$
?	$\pi/2$
?	$\pi/2$
...	...
?	$\pi/2$



MAPPING RULE

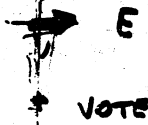
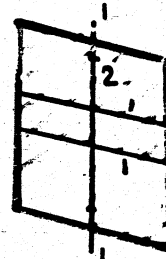
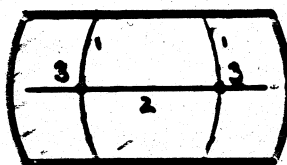
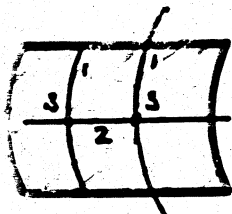
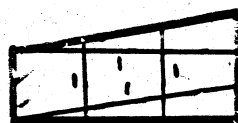
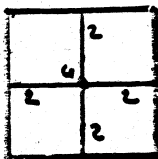
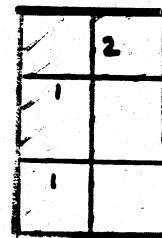
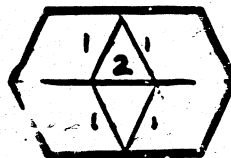
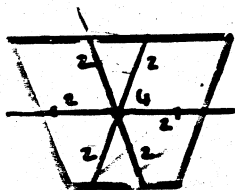


IMAGE AND PARAMETER SPACE



----- EXAMPLE -----

$$\underline{S = 1}$$

ROTATION NOT MEASURED

Mapping function:

$$X_r = X_e - \rho(\theta) \cos \{\theta + \psi_e - \beta(\theta)\}$$

$$Y_r = Y_e - \rho(\theta) \sin \{\theta + \psi_e - \beta(\theta)\}$$

where:

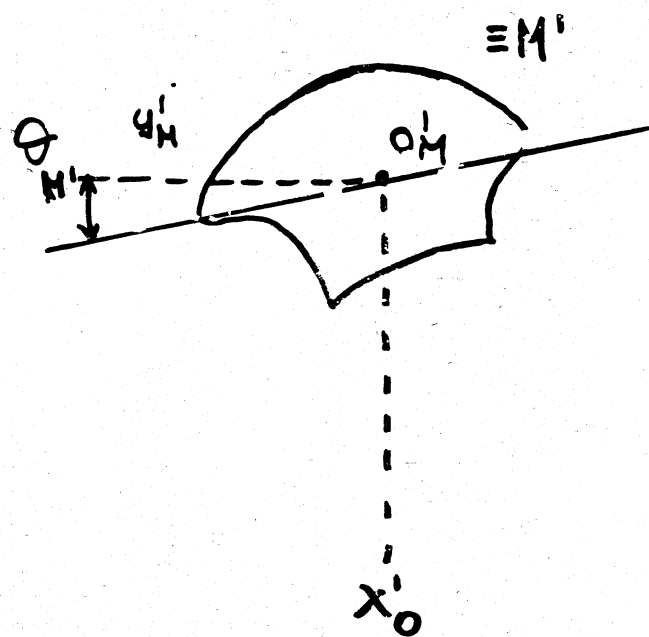
(x_e, y_e) are the picture edge element coordinates

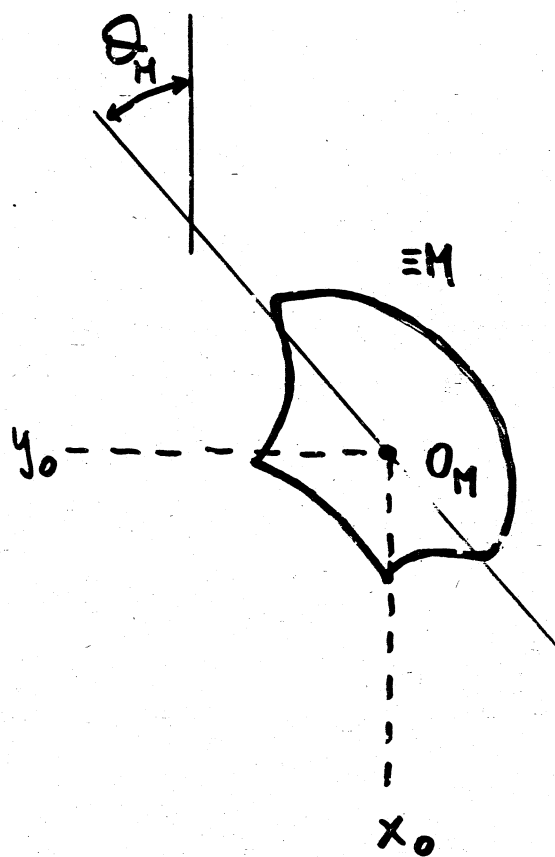
θ is the independent variable

$\rho(\theta)$ is the model description in polar coordinates

$\beta(\theta)$ is the tangent direction of the model in the point ρ, θ

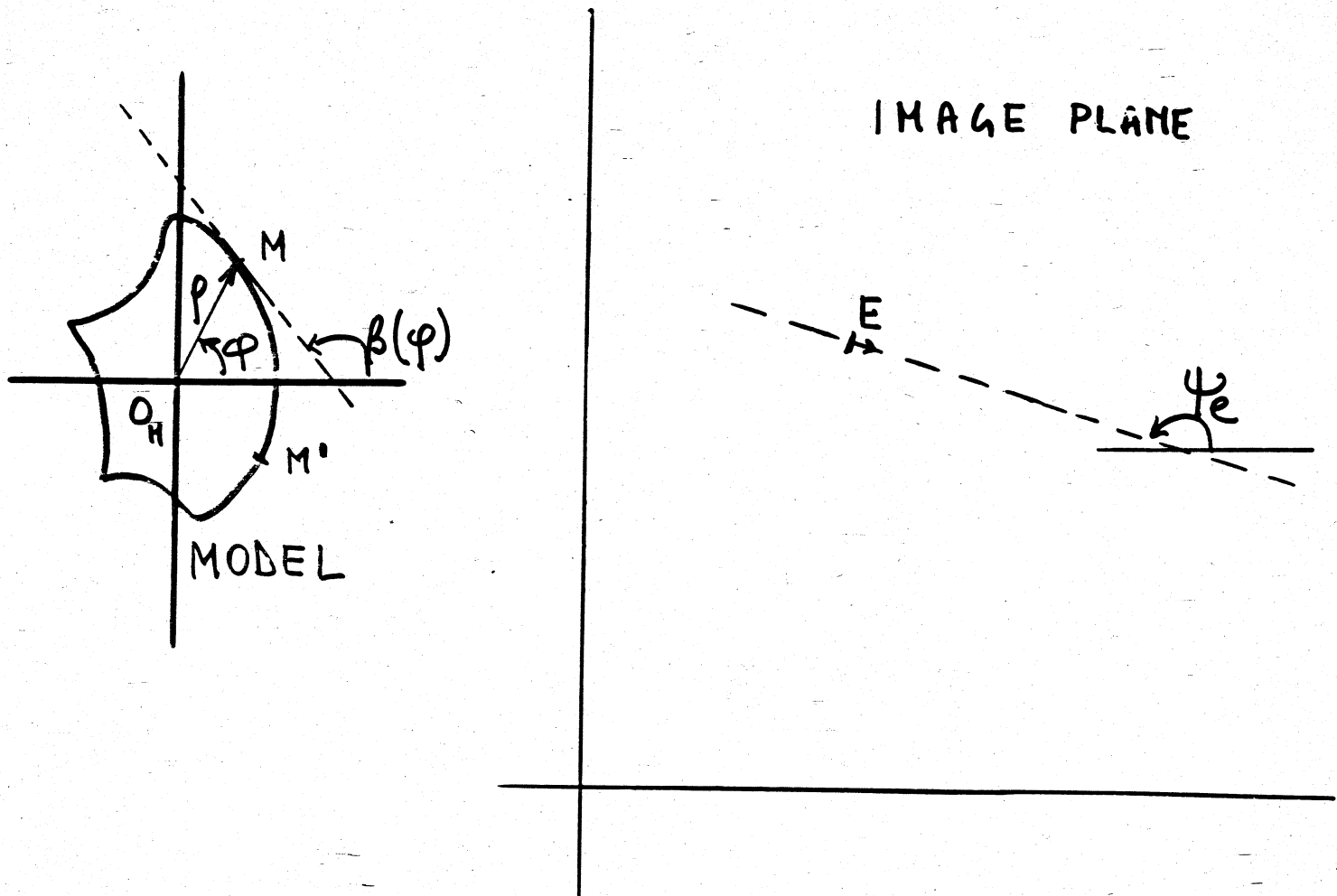
ψ_e is the gradient direction in e .





GENERALIZED HOUGH TRANSFORM

DETECTION AND LOCATION



$$E = (x_e, y_e, \psi_e)$$

$$\left\{ \begin{array}{l} x_o = x_e - \rho(\varphi) \cos[\psi_e + \varphi] \\ y_o = y_e - \rho(\varphi) \sin[\psi_e + \varphi] \\ \theta = \psi_e - \beta(\varphi) \end{array} \right.$$

THE HOUGH TECHNIQUE

BASIC ELEMENTS:

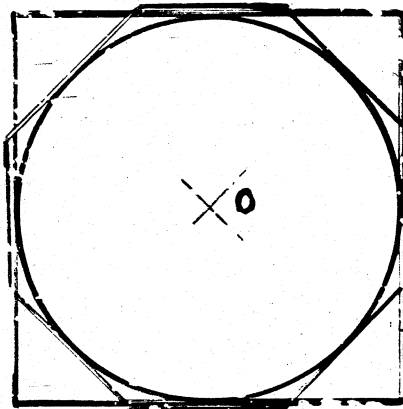
- A) A LOCAL EDGE-DETECTOR ELEMENT, E
- B) AN N-DIMENSIONAL PARAMETER SPACE, P , QUANTIZED AND REPRESENTED BY AN N-DIMENSIONAL ACCUMULATOR ARRAY, AA
- C) A MAPPING, M , FROM THE INFORMATION PROVIDED BY E INTO P
(AND THUS AA)
- D) A VOTING RULE, V , SPECIFYING HOW A PARTICULAR EDGE-ELEMENT AFFECTS THE VALUES OF AA
- E) A DETECTION RULE, D , SPECIFYING THE CONDITIONS UNDER WHICH A PARTICULAR SHAPE HAS BEEN DETECTED.

SELECTION OF THE REFERENCE POINT

HOUGH TRANSFORM

REGULAR POLYGONS

MAPPING RULES



TRANSFORMED SPACE OF HXIN



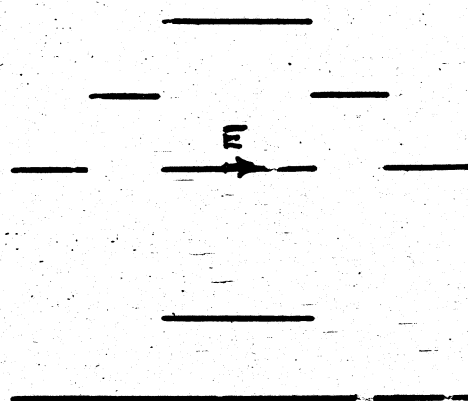
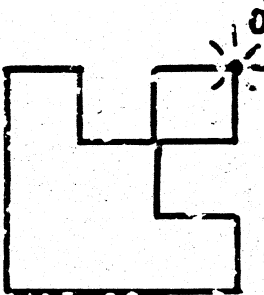
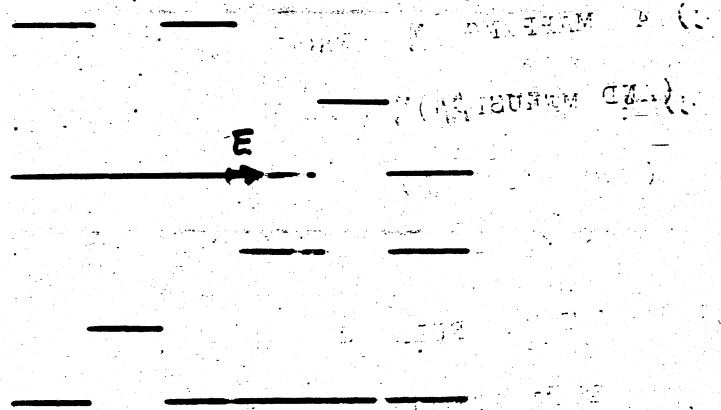
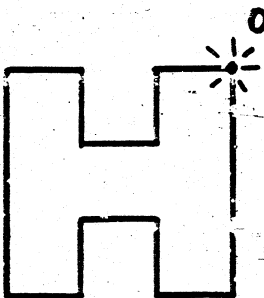
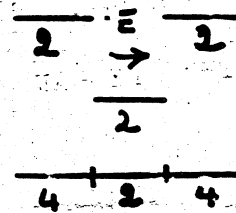
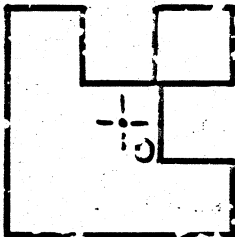
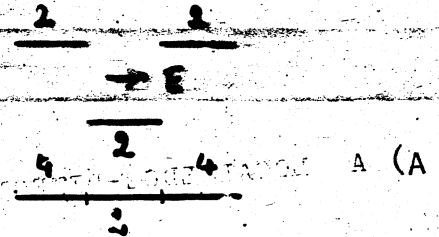
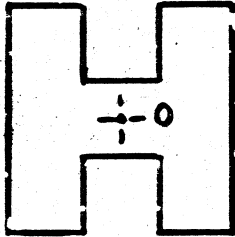
SHAPE	LOCUS M
SEGMENT	SEGMENT
EQUILATERAL TRIANGLE	
SQUARE	SIDE
REGULAR POLYGON	
RECTANGLE	
RHOMBUS	COUPLE OF SIDES
PARALLELOGRAM	
CIRCLE	POINT
POINT	
SYMMETRIC FIGURE	HALF SHAPE

GENERALIZED HOUGH TRANSFORM

SELECTION OF THE REFERENCE POINT

MODEL

HAPPING RULE

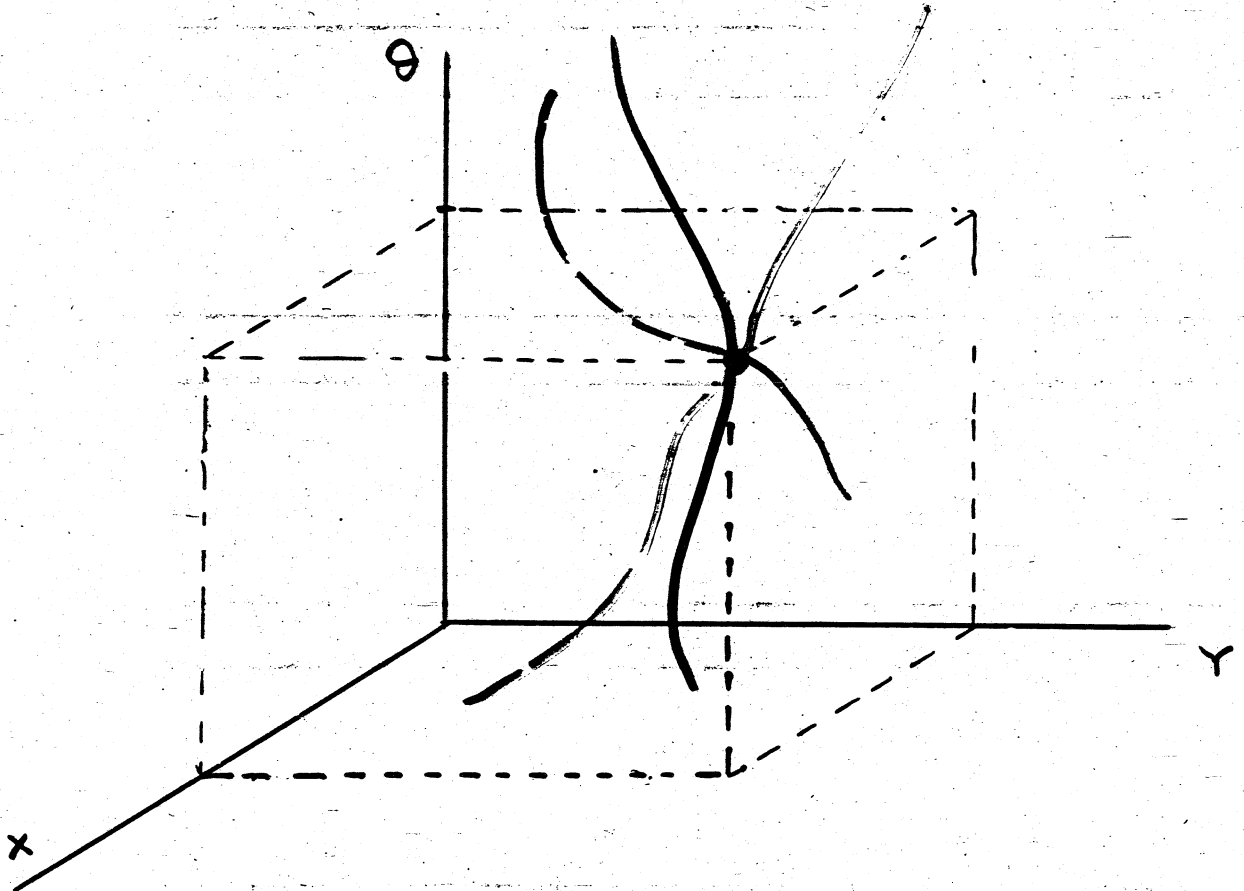


ORIENTATION DETECTION

$$x_0 = x_c - \rho(\varphi) \cos [\psi_c - \beta(\varphi) + \varphi]$$

$$y_0 = y_c - \rho(\varphi) \sin [\psi_c - \beta(\varphi) + \varphi]$$

$$\theta = \psi_c - \beta(\varphi)$$



TRANSFORM

ORIENTATION DETECTION

■ 3D METHOD

$$x_0 = x_c - \rho(\varphi) \cos[\psi_c - \beta(\varphi) + \varphi]$$

$$y_0 = y_c - \rho(\varphi) \sin[\psi_c - \beta(\varphi) + \varphi]$$

$$\theta = \psi_c - \beta(\varphi)$$

ALL VOTES DERIVED FROM THE MAPPING OPERATION WILL BE STORED UP IN THE LOCATION OF THIS 3D SPACE

- THE INDEX PROCESS IS COMPLEX
- IT IS NECESSARY TO SEEK THE PEAK IN A 3D SPACE
- THE ALLOCATION MEMORY IS VERY HIGH

■ 2D AND $2\frac{1}{2}$ METHOD

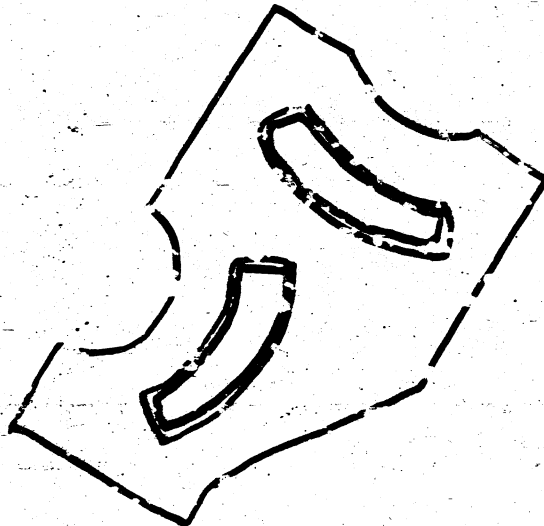
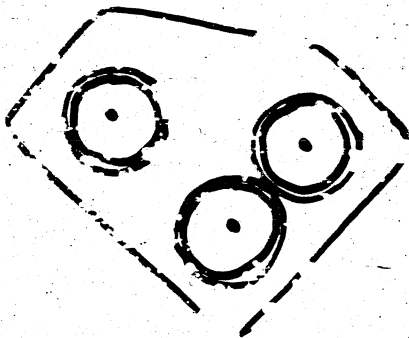
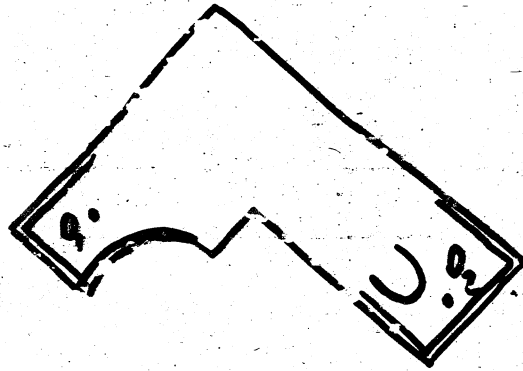
- USING SEVERAL R-TABLES OBTAINED REFERRING THE MODEL TO DIFFERENT REFERENCE POINTS
- USING SEVERAL SUBSHAPE MODELS AND SEVERAL R-TABLES REFERRING EACH SUBMODEL TO ITS OWN REFERENCE POINT

THESE TWO METHODS GIVE IN THE PARAMETER SPACE AS MANY PEAKS AS THE REFERENCE CENTERS USED, AT THE SAME RELATIVE POSITION OF THE CORRESPONDENT CENTER IN THE ORIGINAL MODEL

- THE POSSIBILITY OF WORKING IN A MULTIPROCESSING ENVIRONMENT ALLOWS TO ALLOCATE EACH R TABLE IN DIFFERENT PROCESSORS
- THE KNOWLEDGE OF THE SPATIAL RELATIONS AMONG THE REFERENCE POINTS OF THE SUBSHAPE PERMITS

ORIENTATION DETECTION

- P_1 reference point of the 1st subshape
 P_2 reference point of the 2nd subshape



In a 2D Accumulator we look for more than one maximum points

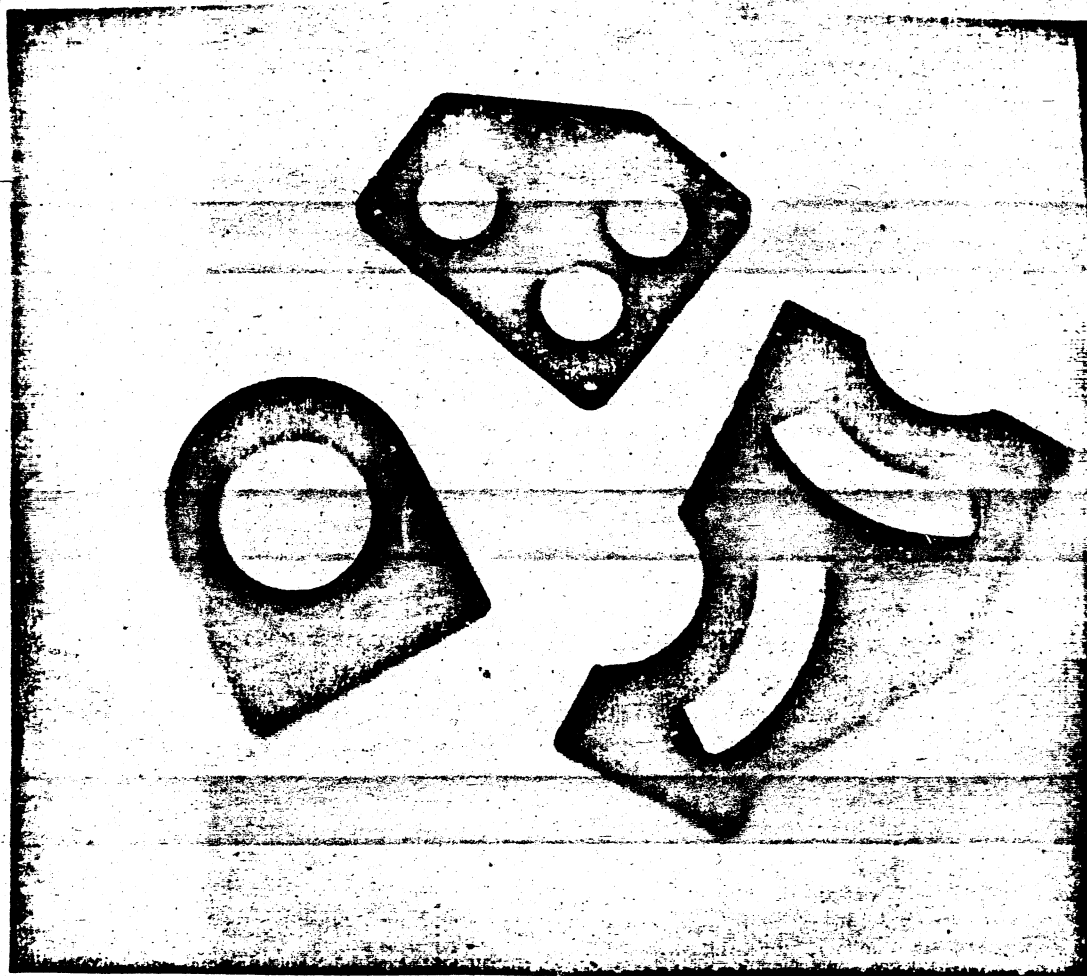
LABELING OF LOCAL INSTANCES

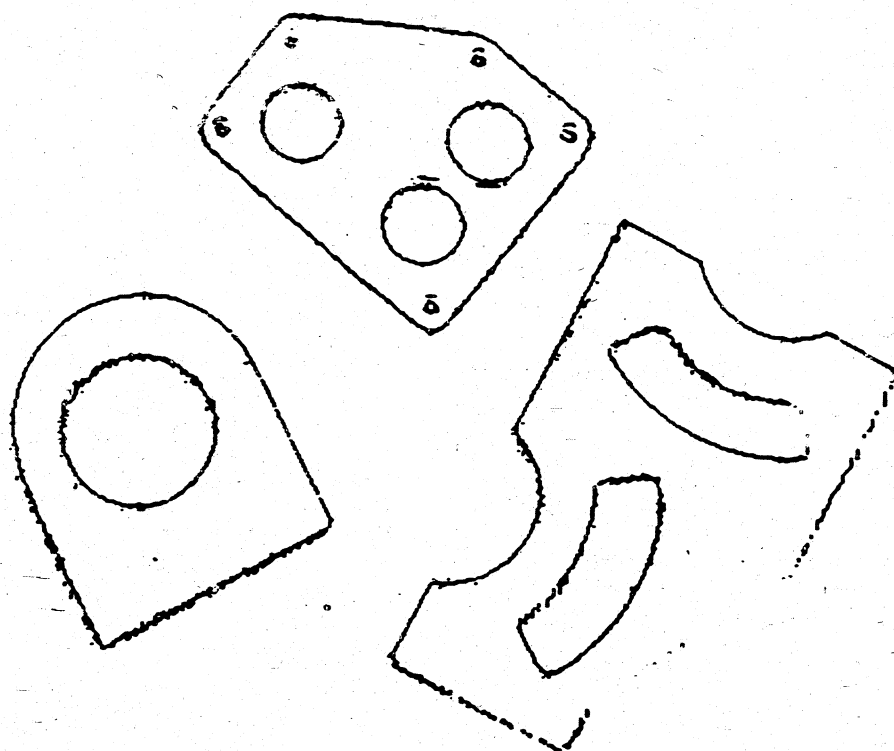
ADVANTAGES

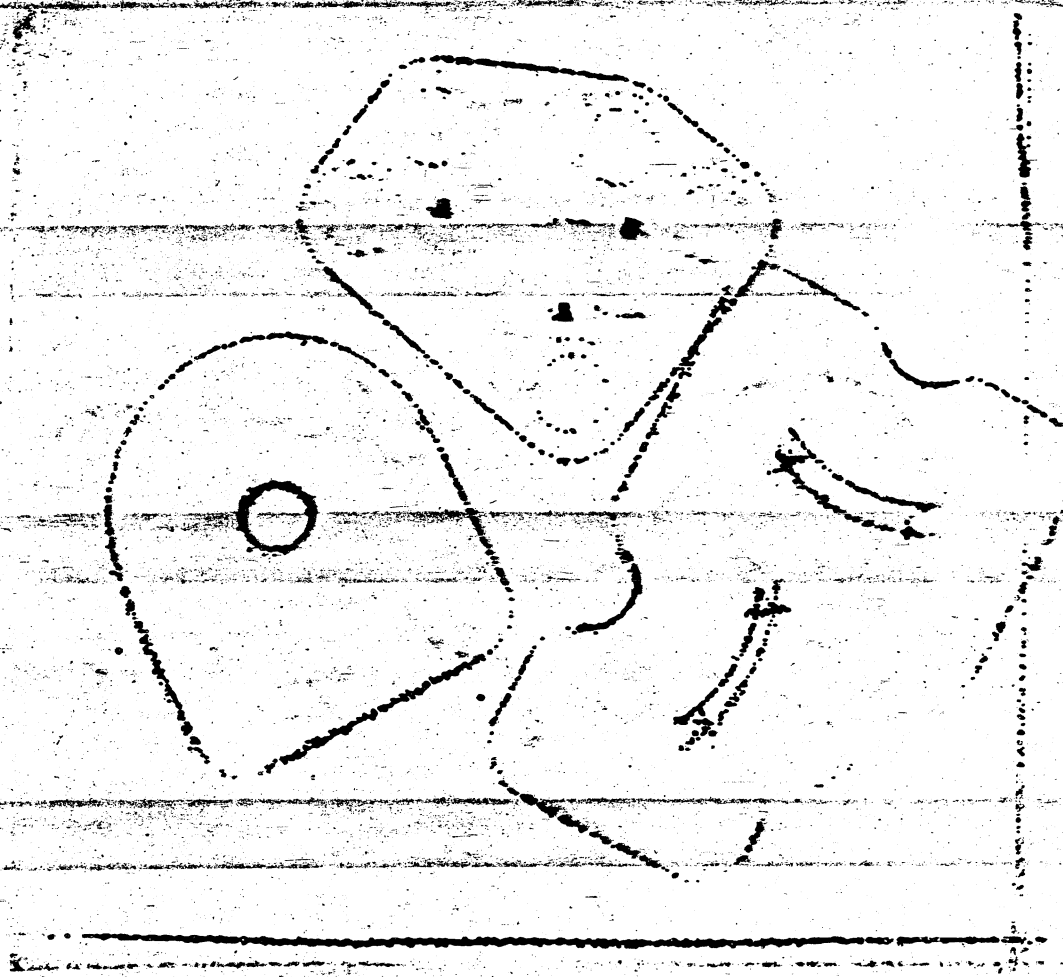
- EXPLOITATION OF THE INFORMATION OF THE "CRITICAL" POINTS (SIDE, CORNER, CONCAVE AND CONVEX PARTS, ETC)
- SPEED UP OF COMPUTATION
(EACH POINT FOR THE INSTANCES HAVING THE SAME LABEL IN THE MODEL)
- THE ANALYSIS OF THE LOCAL CONTEXT IS EASILY IMPLEMENTED IN PARALLEL MACHINES

REQUIREMENTS

- ANALYSIS IN A SUBARRAY LARGER THAN 3×3
- SEVERAL REFERENCE-TABLES
(ONE FOR EACH LABEL)

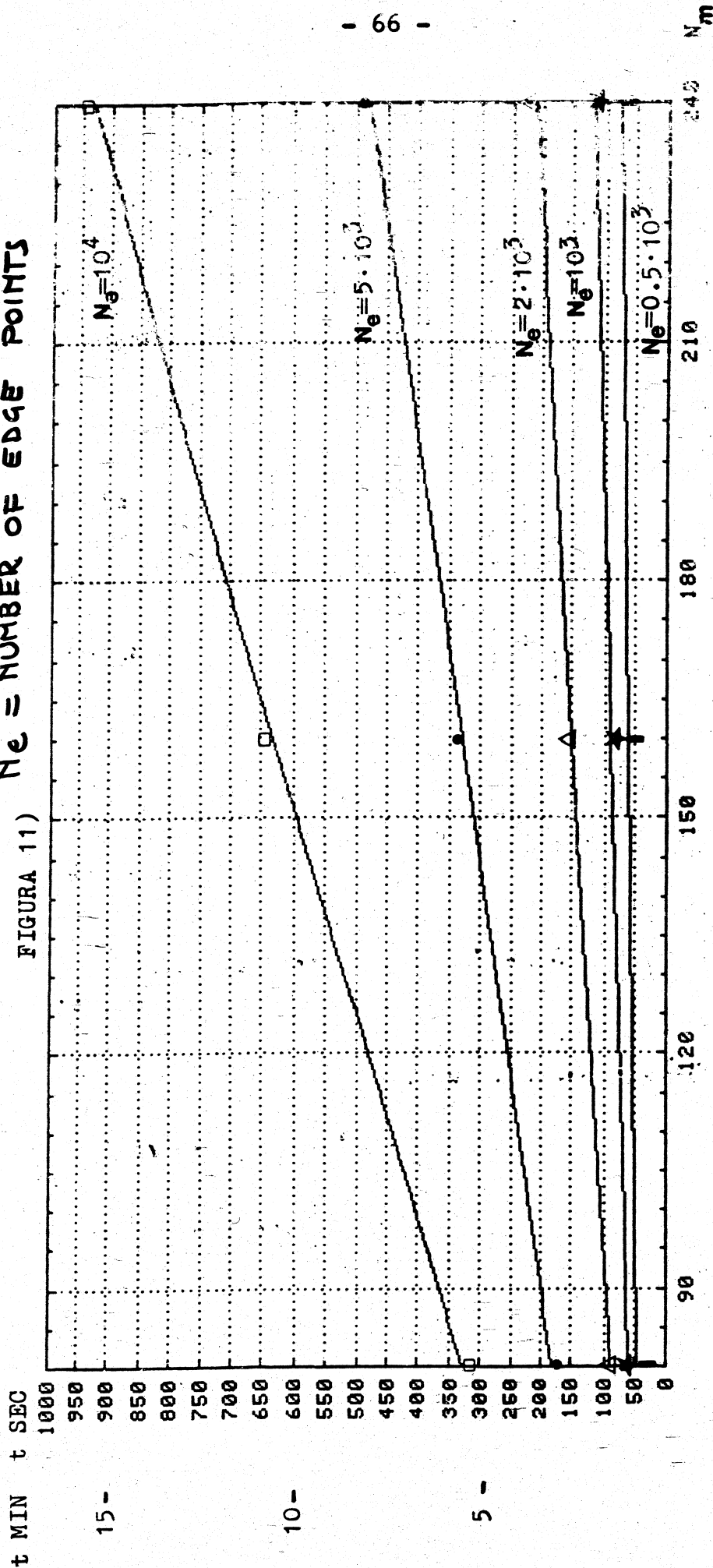






COMPUTATION TIME VERSUS TABLE CARDINALITY

FIGURA 11) N_e = NUMBER OF EDGE POINTS



Tempi di elaborazione

N_e = Numero pixels sede di lato

Valori di t sperimentali:

per immagine da 256x256

N_m = Numero punti del modello

$\square N_e = 10^4$; $\bullet N_e = 5 \cdot 10^3$; $\triangle N_e = 2 \cdot 10^3$

pixels del sistema HP1000F

Valore di t stimato:

$\star N_e = 10^3$; $\blacksquare N_e = 0.5 \cdot 10^3$

$t \approx 30 + 3.75 \cdot 10^{-4} N_m \cdot N_e$ Sec.

MULTI RESOLUTION IMPLEMENTATION

- THE CARDINALITY OF THE REFERENCE TABLE LINEARLY DEPENDS ON THE IMAGE RESOLUTION
- IMPLEMENTING THE HOUGH TRANSFORM IN A PYRAMID DATA STRUCTURE THE HIGHER IS THE PROCESSING LEVEL PLANE THE LOWER IS THE COMPUTATION REQUESTED
$$(H' = H / 2^{l-l'})$$
- USING THE LABELING APPROACH THE COMPUTATION IS PERFORMED AT THE HIGHER RESOLUTION LEVELS ONLY FOR THE ANALYSIS OF POINTS THAT HAVE "COMPLEX" LOCAL CONTEXT

