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Shape extraction



Edge detection



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Segmentation

- ❖ Image segmentation consists into the decomposition of the image in segments (i.e. components)
- ❖ This process is based on a given criteria of homogeneity (chromatic, morphologic, motion, depth, etc.)
- ❖ From the operational viewpoint, three approach have been proposed:
 - ☞ Clustering image data and growing regions
 - ☞ Border following
 - ☞ Search of borders



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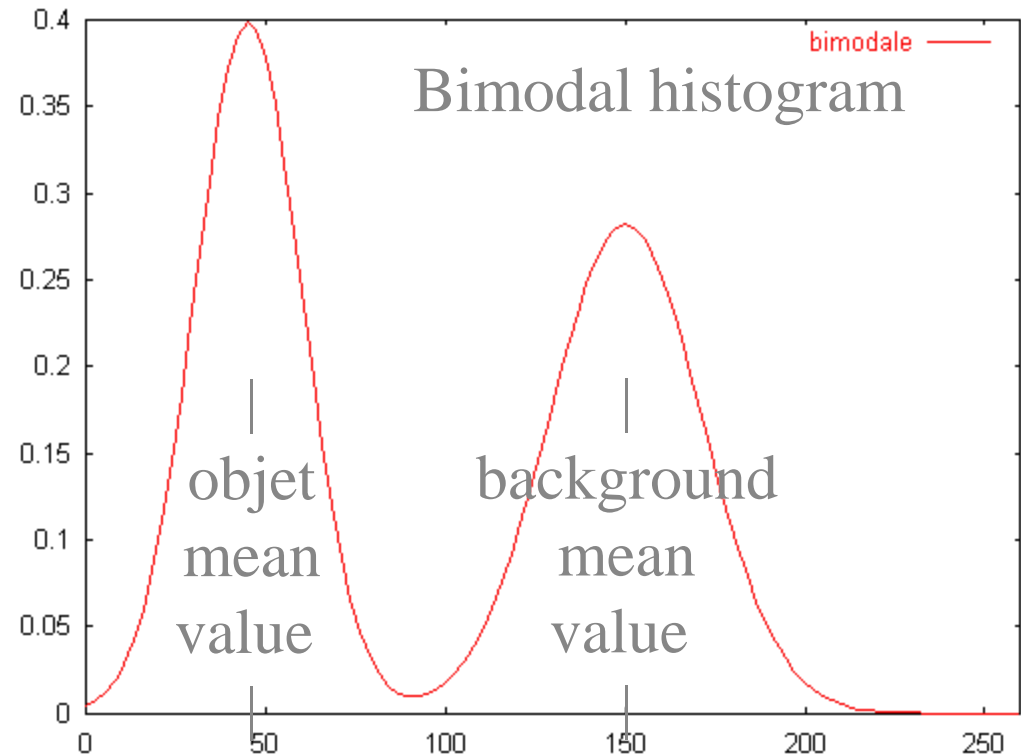
Binary Images

- ❖ The segmentation process leads to detect an individual object (foreground) in contrast to the background so it is a binarization process
- ❖ Some applications are by nature binary: black and white printing, writing, mechanical parts, bio-imagery like cells or chromosomes, etc.
- ❖ Often the originals contains various grey levels due to:
 - ☞ Electric noise of the camera
 - ☞ Non-uniform scene illuminations
 - ☞ Shadowing
 - ☞ ...

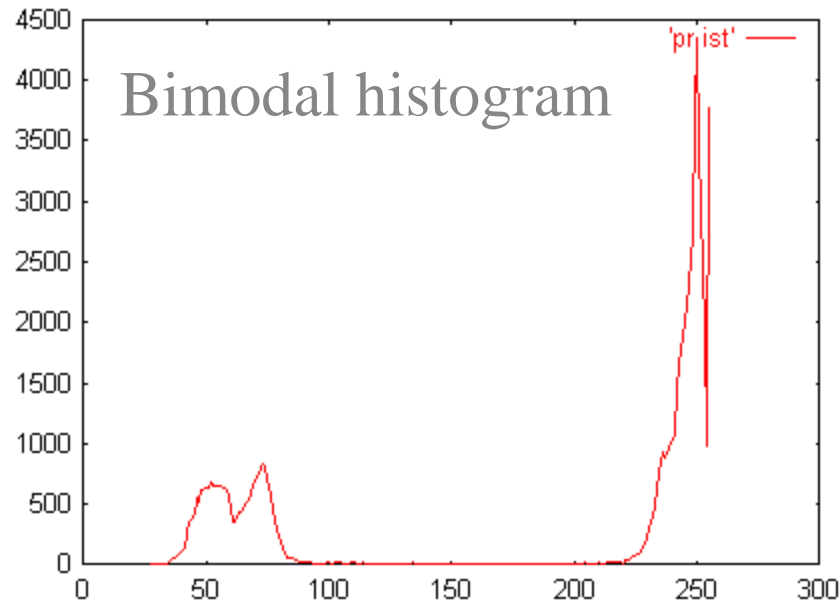


Bimodal Distribution

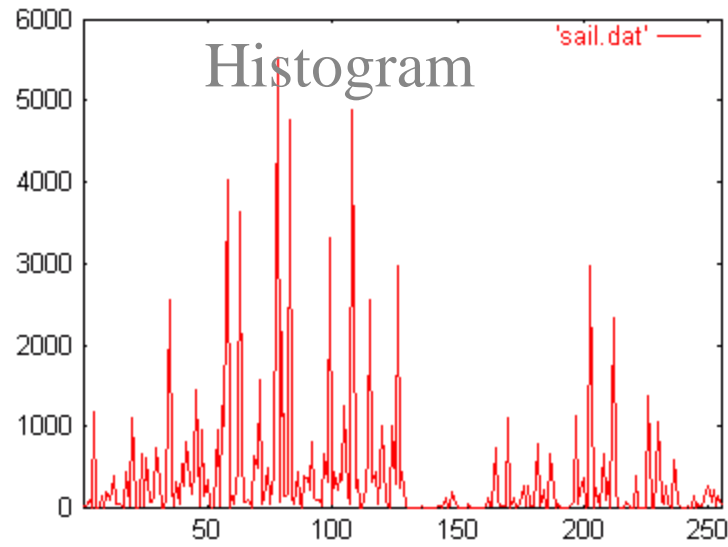
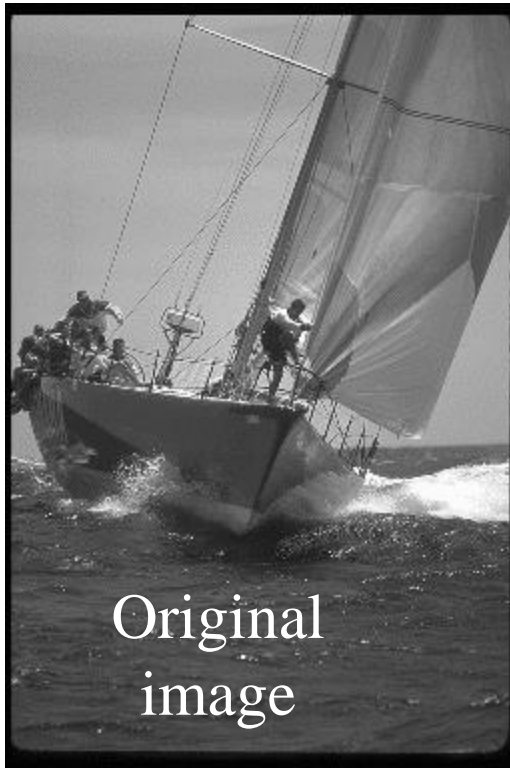
- ❖ The easiest solution is a threshold applied to the grey levels:
 - ☞ $O(i, j) = 0$ se $I(i, j) < S$
 - ☞ $O(i, j) = 255$ otherwise
- ❖ It is required the evaluation of the optimal threshold S .
- ❖ Operating on the histogram, there are two possibilities:
 - ☞ Finding the minimum
 - ☞ Applying statistic criteria



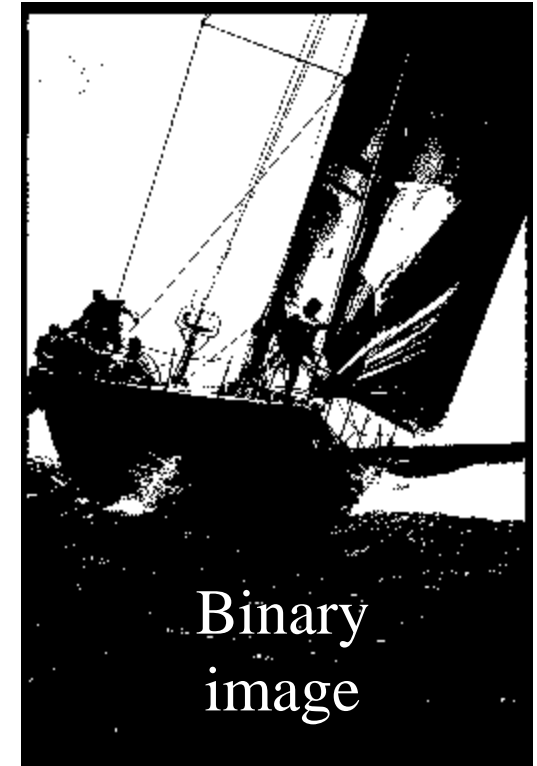
Example: mechanical part



Example: sailing

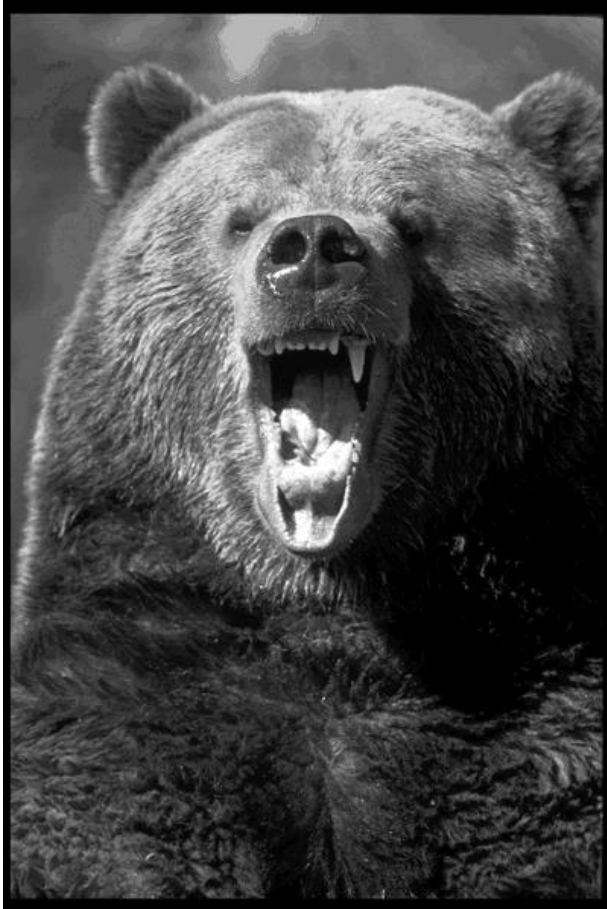


Threshold = 140

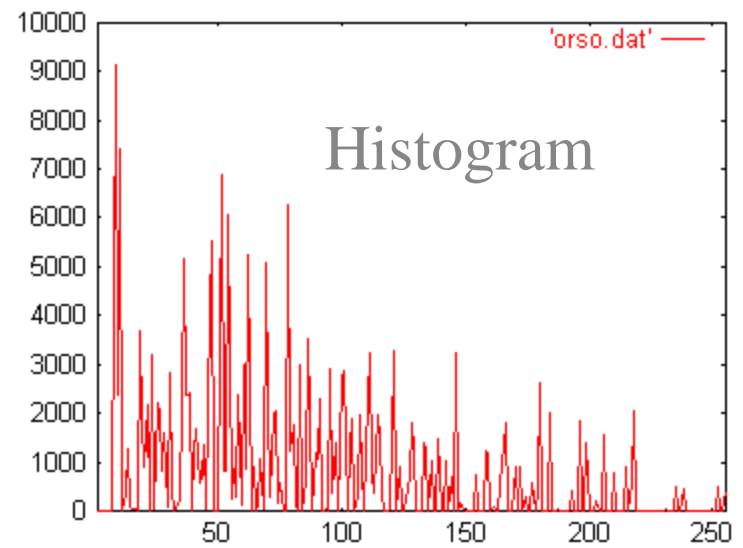


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Example: bear

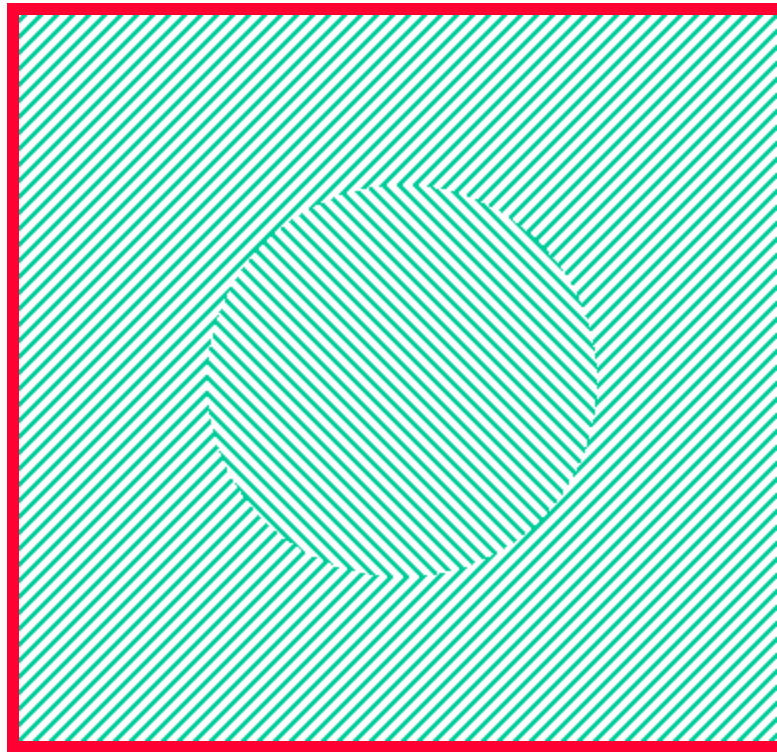


Original image



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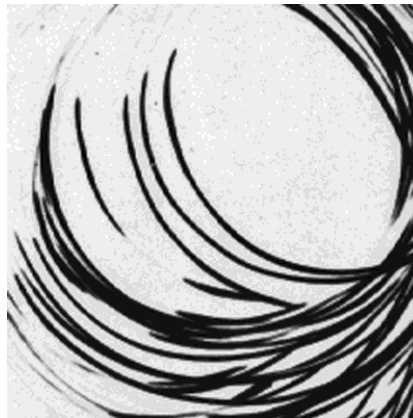
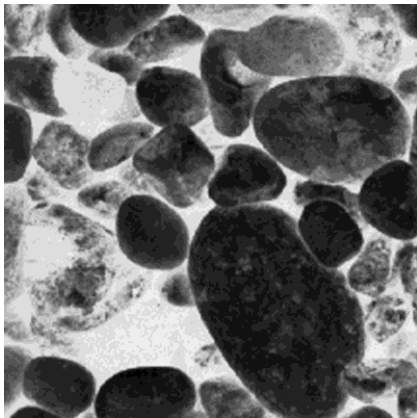
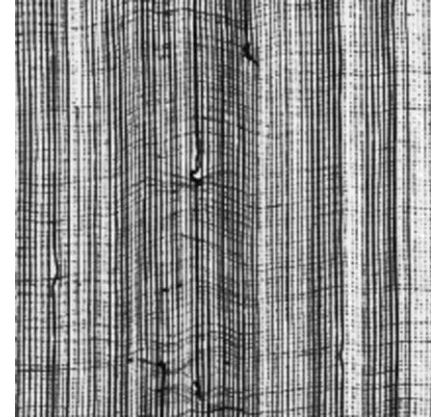
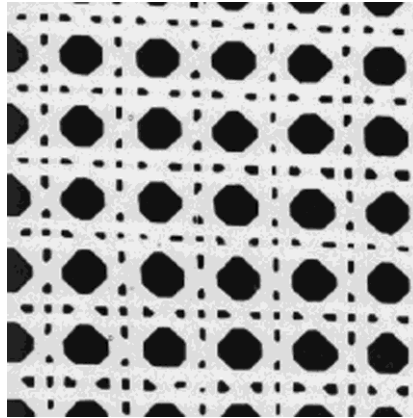
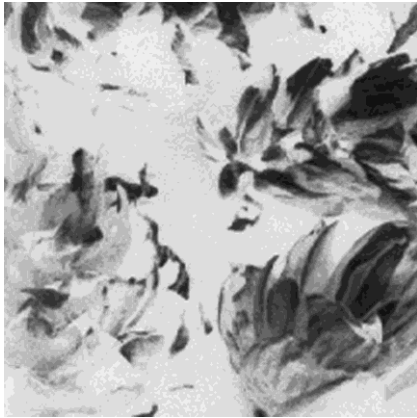
Example: circle



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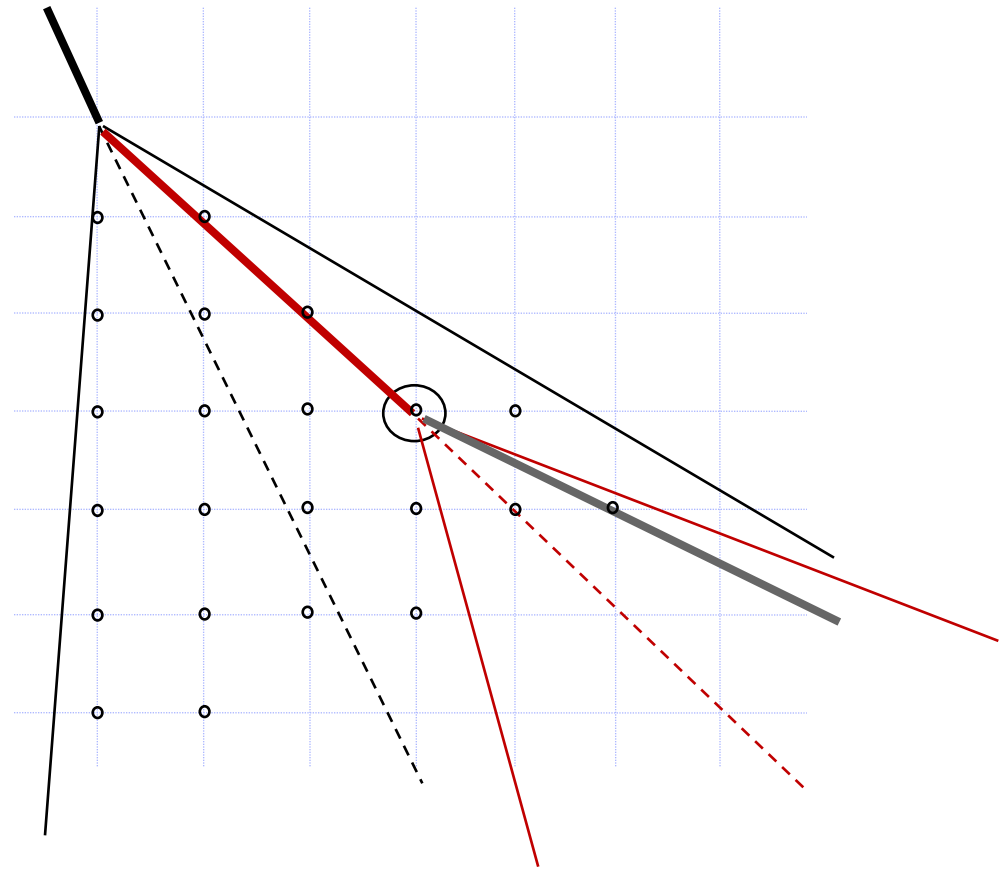
Texture: Brodatz album



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Border following

- ❖ An example of a recursive walk over the image, following the contour to be exhibited. The horizon of an edge point is the triangle of depth 5 and basis 6, in the direction of the last found edge segment.



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Search of borders



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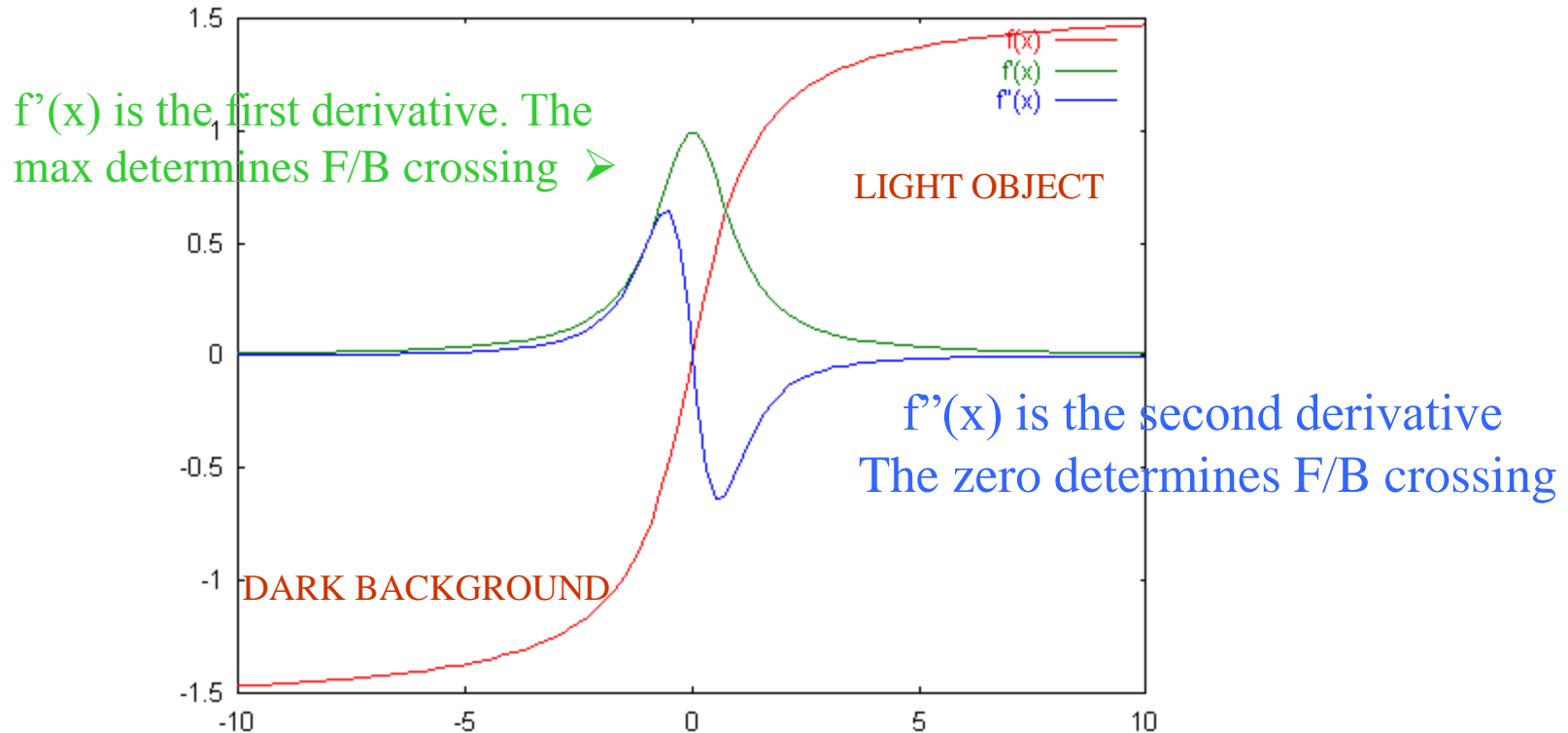
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Analytic derivative model

- ❖ The border search can be based on the discontinuity of an image feature like the grey level, a texture or a motion parameter, the depth in the scene, etc.
- ❖ For operators stemming from first order partial derivatives a maximum response is looked for, either local maximum or over a threshold whether given or adapted
- ❖ Note that the second derivative is used too, and among second order operators the Laplacian is peculiarly popular as being scalar then isotropic. There, of course, the zero crossing – inflection points - are looked for



Analytic derivative model



$f(x)$ is the grey level,
here representing the
image in one dimension

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Analytic derivative model

❖ The first derivative is given by:

$$f'(x) \approx \frac{f(x+h) - f(x-h)}{2h}$$

❖ The second derivative is given by:

$$f''(x) \approx \frac{f(x+h) - 2f(x) + f(x-h)}{h^2}$$

❖ In 2D the derivative is substituted by the vector gradient

Convolution

- ❖ The convolution is a linear operator, that is applied when the image $I(x, y)$ is continuous. To the digital image $I(i, j)$ a filter is applied represented by the mask:

$$O(x_0, y_0) = \iint f(x_0 - x, y_0 - y) I(x, y) dx dy$$

$$O(x, y) = \sum \sum f(x - i, y - j) I(i, j)$$

1	2	3	3	2	3
3	2	5	2	7	6
1	3	6	7	8	8
1	2	8	9	6	7
2	3	7	7	6	8
3	3	8	9	8	8

	26	33	43	46	
	31	44	58	60	
	33	52	64	66	
	37	50	68	68	

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Convolution (decomposition)

❖ In general the convolution is a computer demanding operator, e.g. the 5x5 template:

$$\begin{matrix}
 1 & 4 & 6 & 4 & 1 \\
 4 & 16 & 24 & 16 & 4 \\
 6 & 24 & 36 & 24 & 6 \\
 4 & 16 & 24 & 16 & 4 \\
 1 & 4 & 6 & 4 & 1
 \end{matrix}$$

is implemented by 25 multiplications for each pixel; note that often complex template may be decomposed in simple 1D operators (e. g. the isotropic, monotonic decreasing template)

❖ The previous convolution can be decomposed in the following two 1D operators:

$$\begin{matrix}
 1 & 4 & 6 & 4 & 1 \\
 \text{et} & & & & \\
 & & & & 1 \\
 & & & & 4 \\
 & & & & 6 \\
 & & & & 4 \\
 & & & & 1
 \end{matrix}$$

in this implementation only 10 (5+5) multiplications per pixel are required

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Gradient approximations

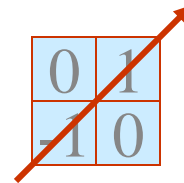
- ❖ The gradient is a 2D vector
- ❖ The digital differential operators are implemented by template in **which the sum of the kernel parameters is null**: in a uniform area the result must be zero (no variation)
- ❖ The basic and historical convolution kernels have an extension limited to 2x2 and 3x3, for each of the two components

Roberts Operator

❖ It is the simplest solution

- ☞ Two templates are applied M_1 and M_2 , obtaining the two orthogonal gradient components:
- ☞ $G_1 = M_1 * I$, $G_2 = M_2 * I$
- ☞ It is very sensible to noise

G_1

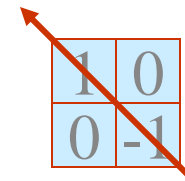


❖ The gradient module and phase are:

$$G_m = \sqrt{G_1^2 + G_2^2}$$

$$G_\phi = \arctg(G_2/G_1) + \pi/4$$

G_2



Isotropic operator

- ❖ Two templates are applied M_1 and M_2 , obtaining the two orthogonal gradient components:

$$G_x = M_x * I, G_y = M_y * I$$

- ❖ The gradient module and phase are:

$$G_m = \sqrt{G_1^2 + G_2^2}$$

$$G_\phi = \text{arctg}(G_y/G_x)$$

- ❖ In C:

☞ $\text{phi} = \text{atan2}(g_y, g_x)$


$$G_x \rightarrow \begin{bmatrix} -1 & 0 & 1 \\ -\sqrt{2} & 0 & \sqrt{2} \\ -1 & 0 & 1 \end{bmatrix}$$


$$G_y \uparrow \begin{bmatrix} 1 & \sqrt{2} & 1 \\ 0 & 0 & 0 \\ -1 & -\sqrt{2} & -1 \end{bmatrix}$$

Prewitt and Sobel operators


- ❖ To simplify the computation often the isotropic filter is implemented by these two simplified solutions:


☞ Prewitt

$$G_x \begin{array}{|c|c|c|} \hline -1 & 0 & 1 \\ \hline -1 & 0 & 1 \\ \hline -1 & 0 & 1 \\ \hline \end{array}$$


$$G_y \begin{array}{|c|c|c|} \hline 1 & 1 & 1 \\ \hline 0 & 0 & 0 \\ \hline -1 & -1 & -1 \\ \hline \end{array}$$


☞ Sobel

$$G_x \begin{array}{|c|c|c|} \hline -1 & 0 & 1 \\ \hline -2 & 0 & 2 \\ \hline -1 & 0 & 1 \\ \hline \end{array}$$


$$G_y \begin{array}{|c|c|c|} \hline 1 & 2 & 1 \\ \hline 0 & 0 & 0 \\ \hline -1 & -2 & -1 \\ \hline \end{array}$$


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Example Sobel



Original image



Module



Phase

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Example Sobel



Original image



Module



Phase

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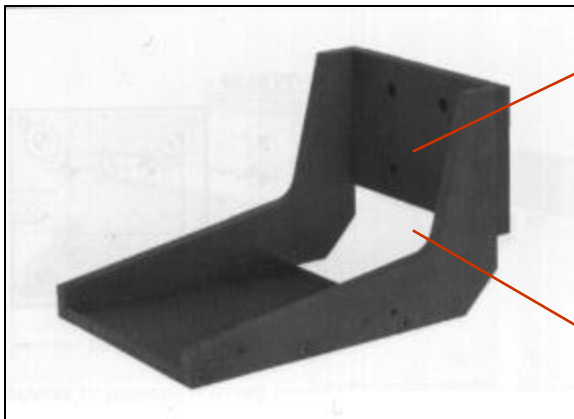
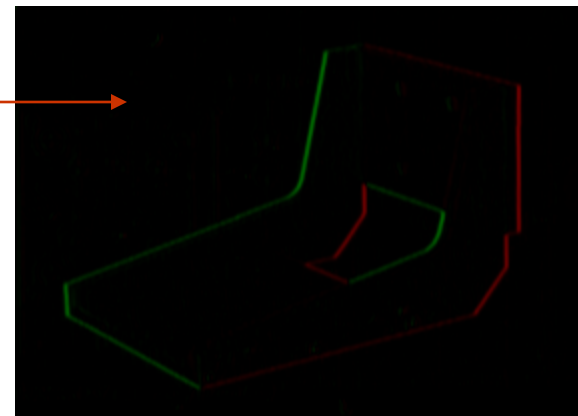
Sobel operator

horizontal gradient

vertical contour

G_1

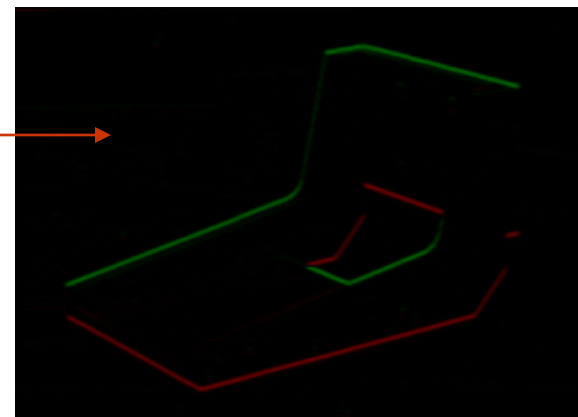
-1	0	1
-2	0	2
-1	0	1



Original image

G_2

1	2	1
0	0	0
-1	-2	-1

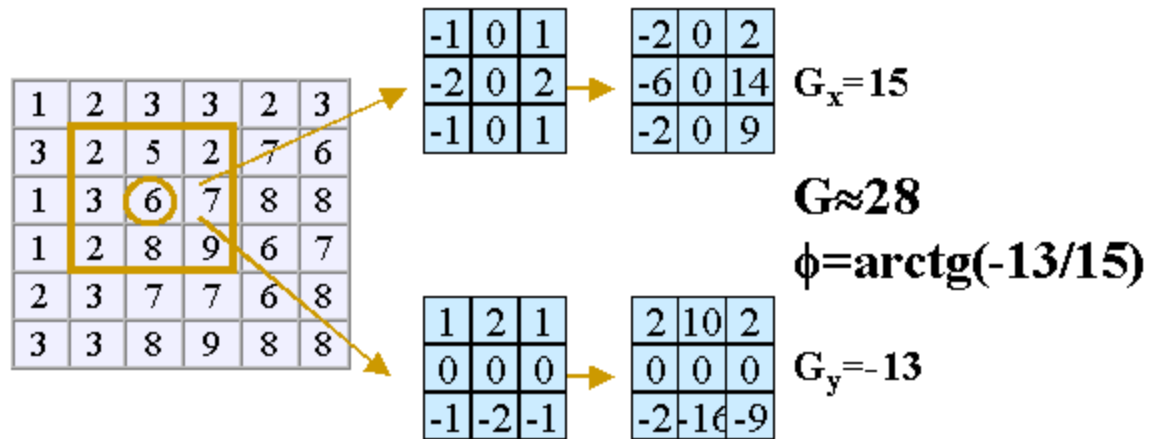
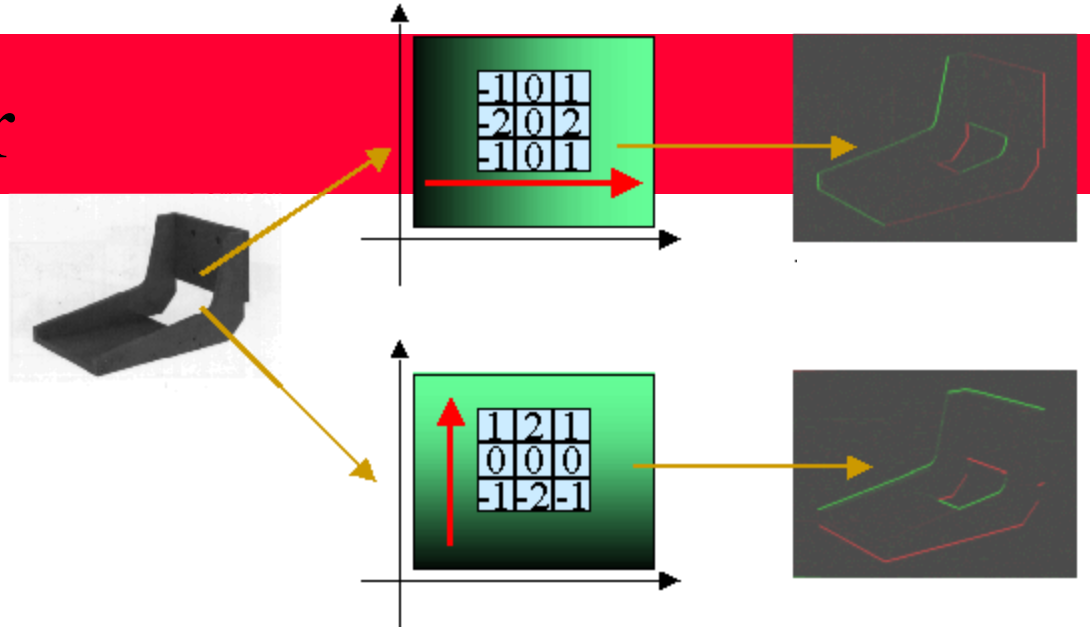


vertical gradient

horizontal contour

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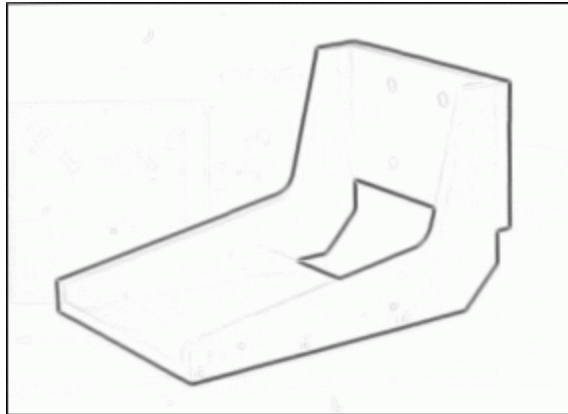
Sobel operator



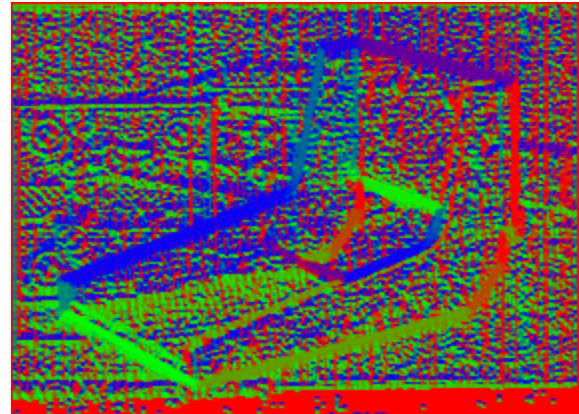
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Sobel operator

Module



Phase



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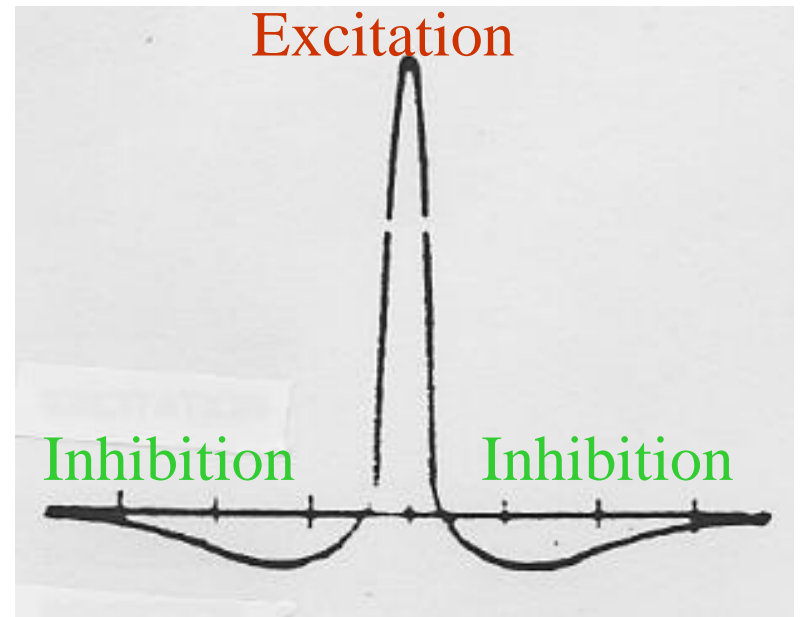
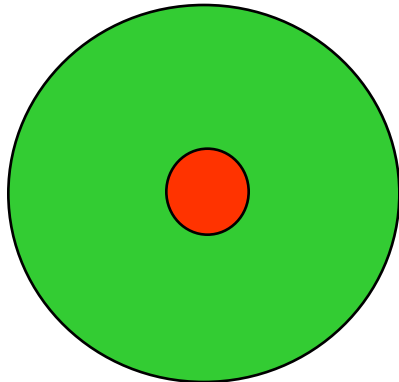
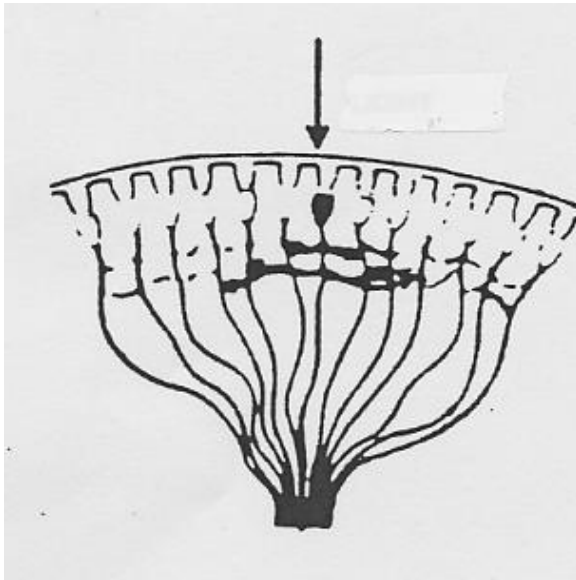
Example (module)



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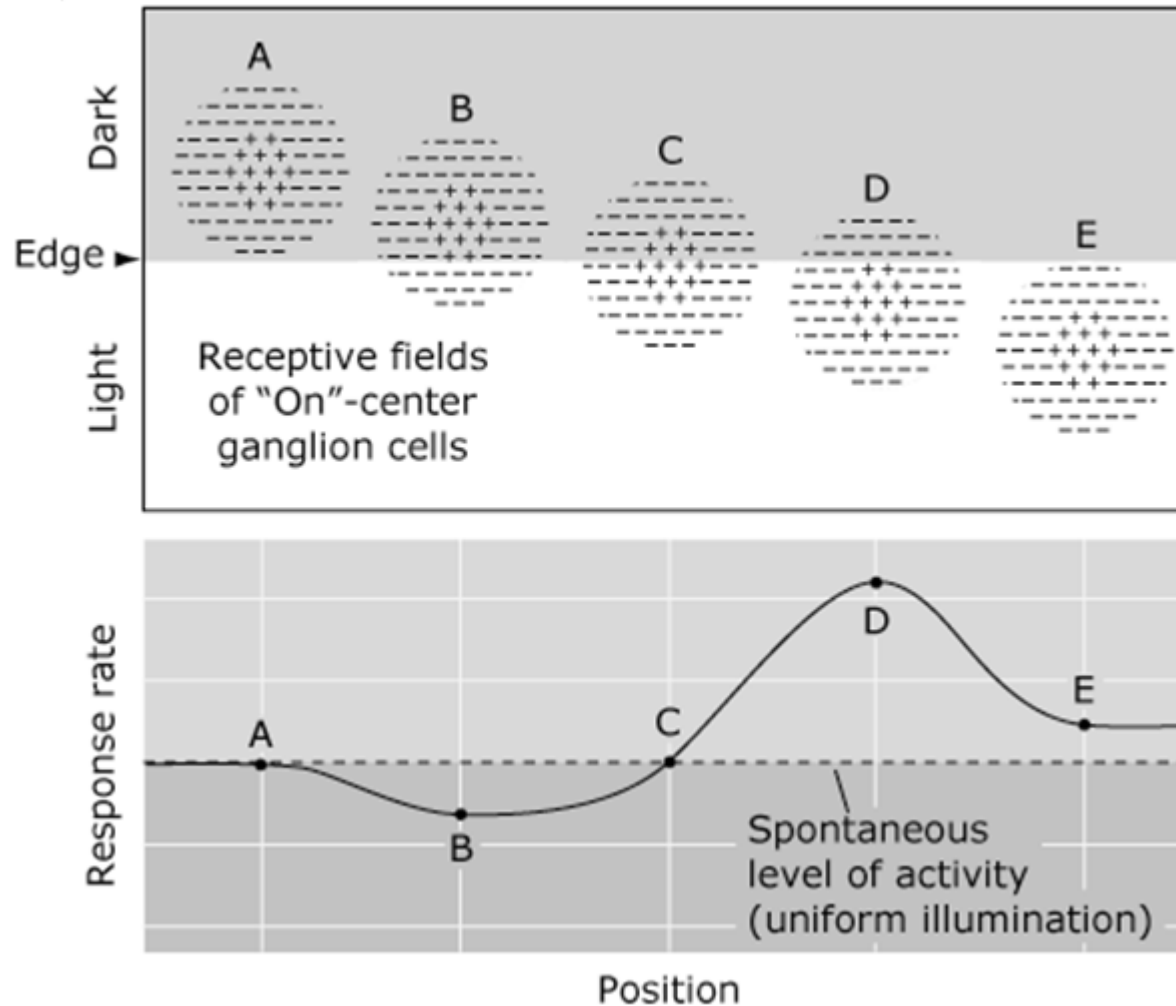
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Lateral inhibition



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Lateral inhibition



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Lateral inhibition

- ❖ The retina receptor apply a lateral inhibition mechanism.
- ❖ The implementation of this mechanism can be done by a filter obtained by the difference of two Gaussian of equal area, having different σ (and amplitude):

$$\frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

- ❖ The 'zero-crossing' correspond to the border points. An advantage of this technique is that the produced contour are closed.

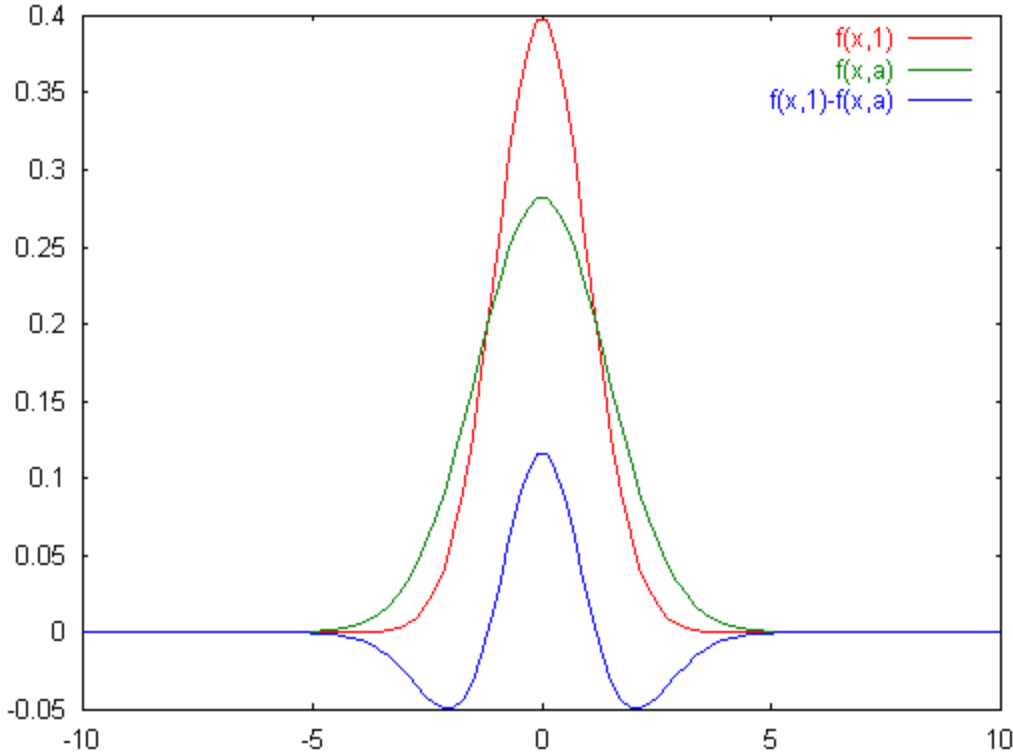
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The DoG operator

- ❖ This operator is called usually Difference of Gaussians (DoG)
- ❖ The best results are obtained maintaining the external Gaussian as large as possible but avoiding to include more than one border
- ❖ The internal Gaussian is optimized if it covers just the transition area
- ❖ Complex scene are better analyzed if a set of different DoG filters with various σ are applied.

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The DoG operator



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DoG Example



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DoG Example



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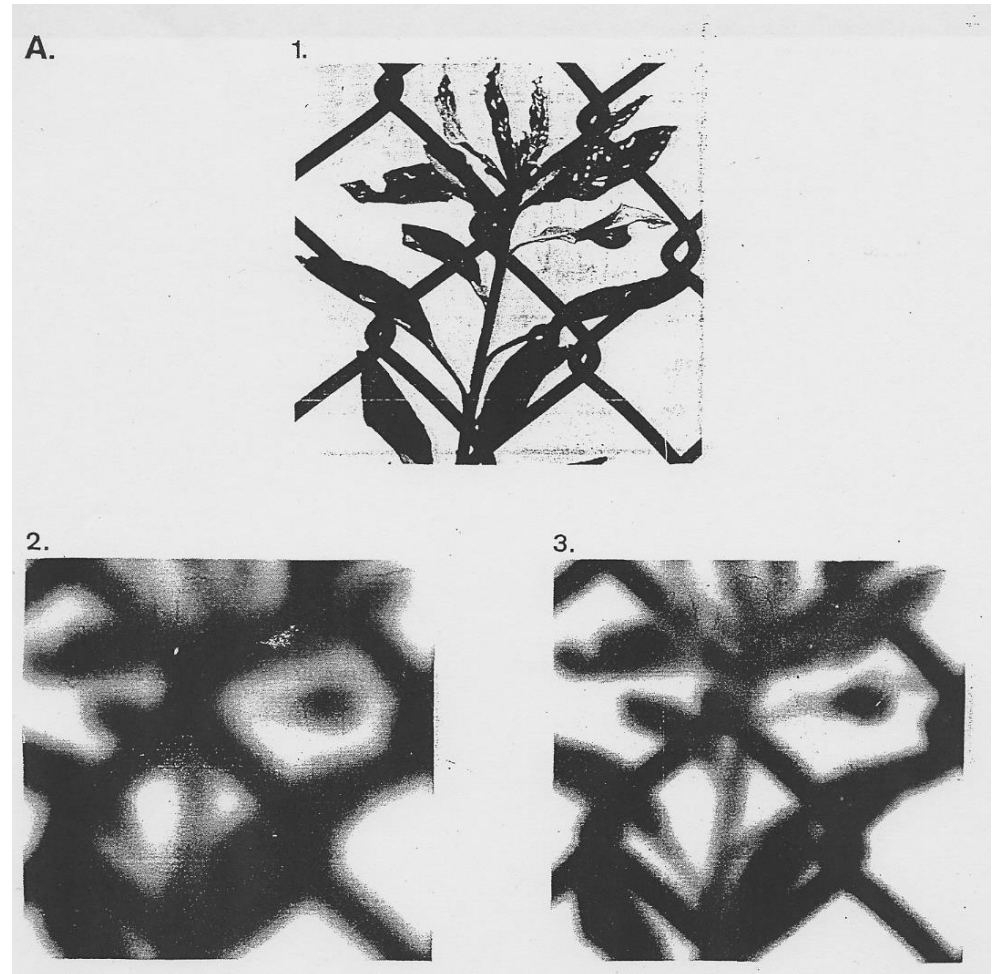
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Gaussian Filter

1 Original image

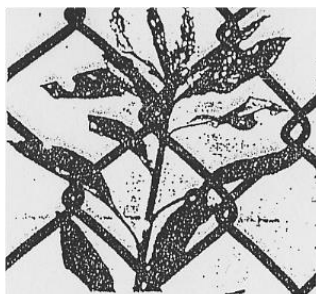
2 Filtered image $\sigma=8$

3 Filtered image $\sigma=4$

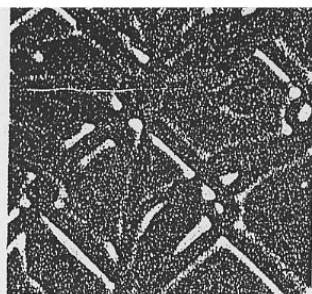


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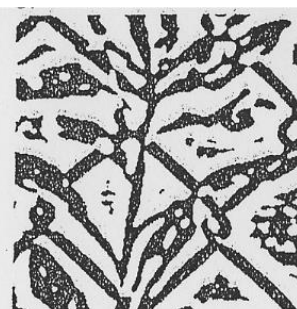
DoG Filter



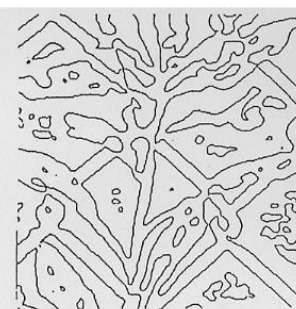
Original



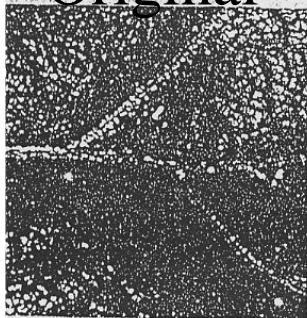
Filtered



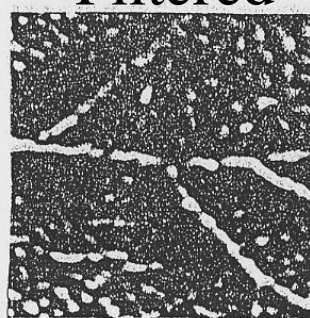
Threshold = 0



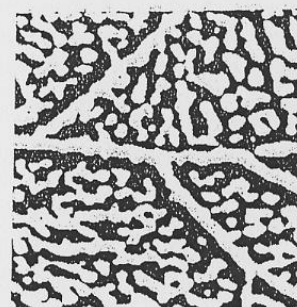
Contour



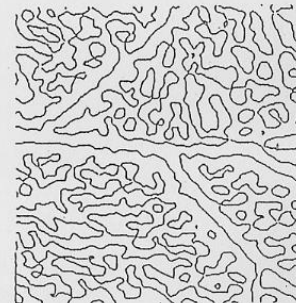
Original



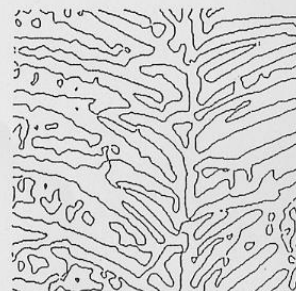
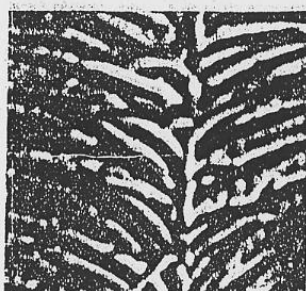
Filtered



Threshold = 0



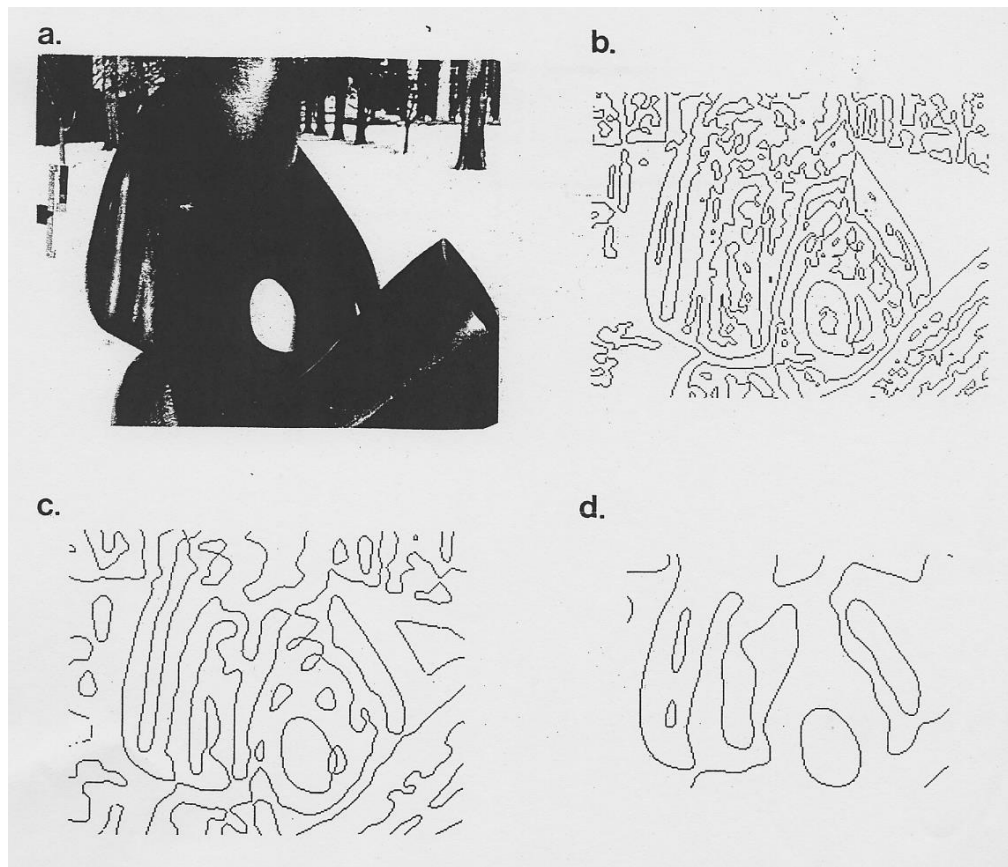
Contour



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DoG: σ dependence

Original



$\sigma = 12$

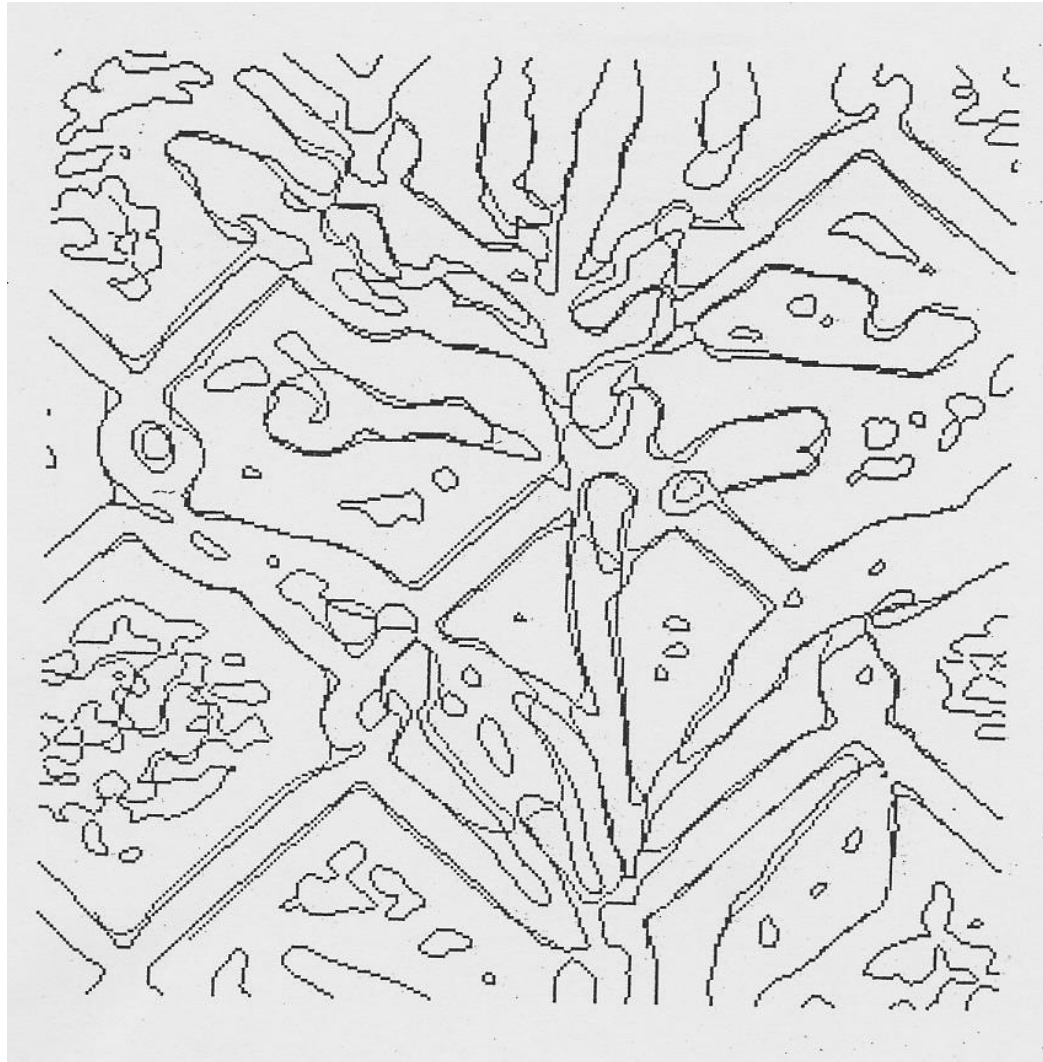
$\sigma = 6$

$\sigma = 24$

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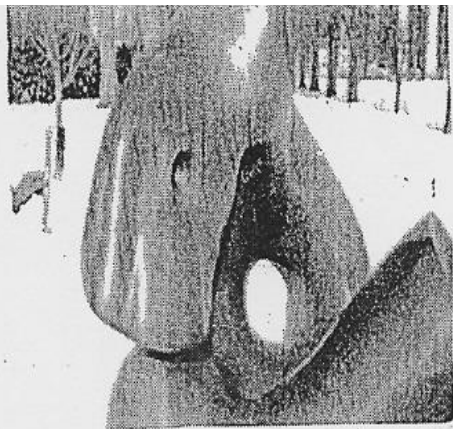
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DoG: contour robustness



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DoG: discretization of grey level and noise



Original



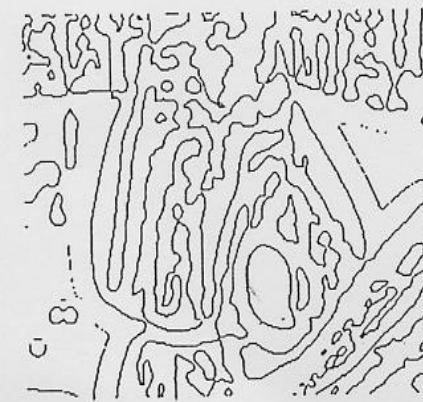
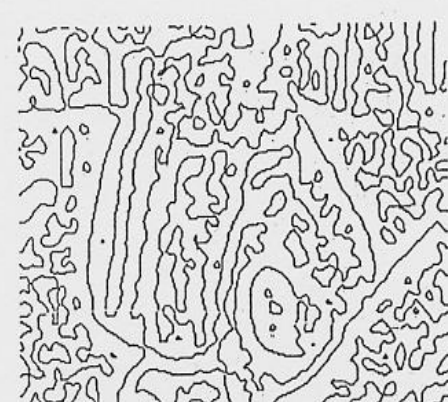
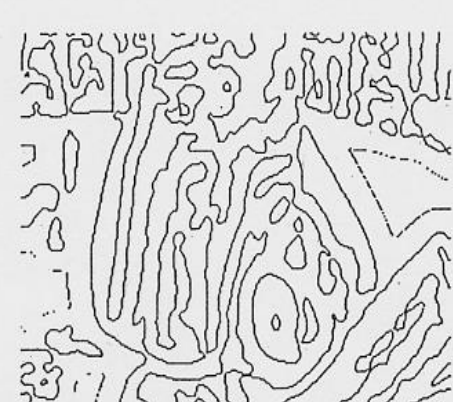
with noise



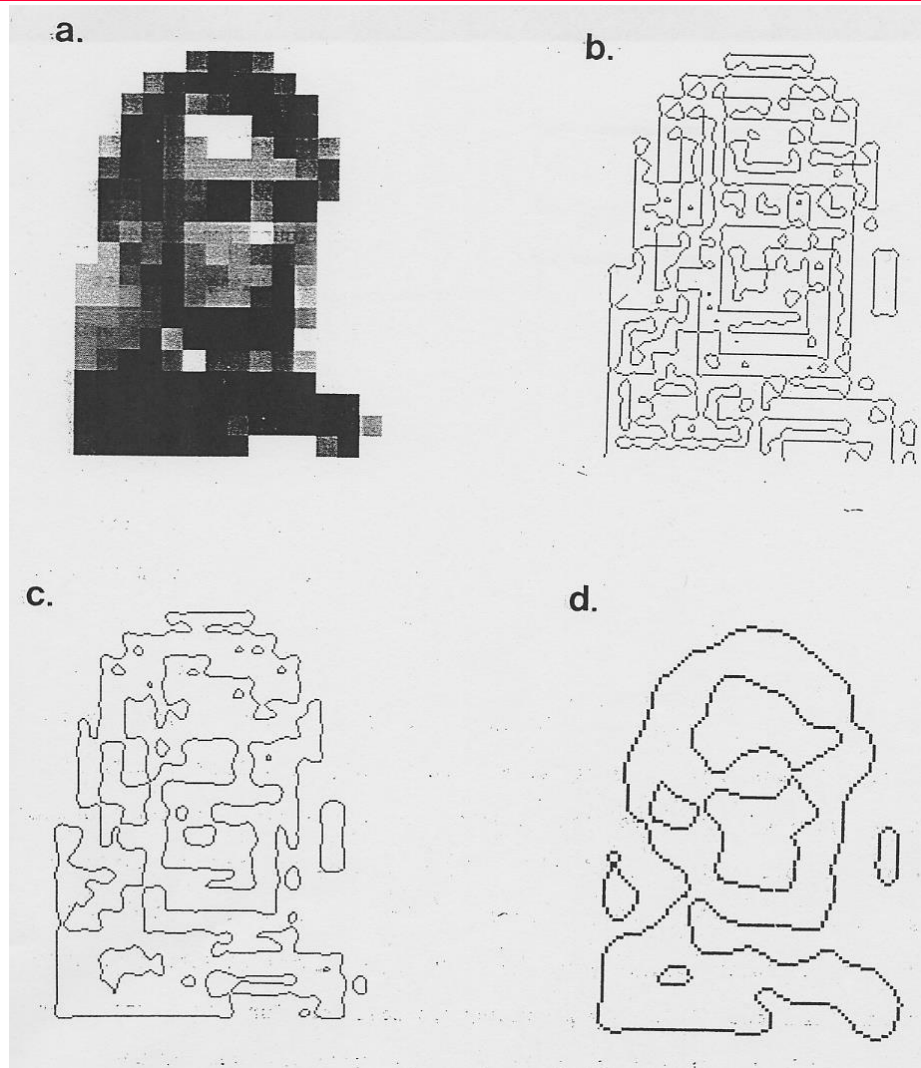
16 grey levels



8 grey levels



DoG: spatial discretization



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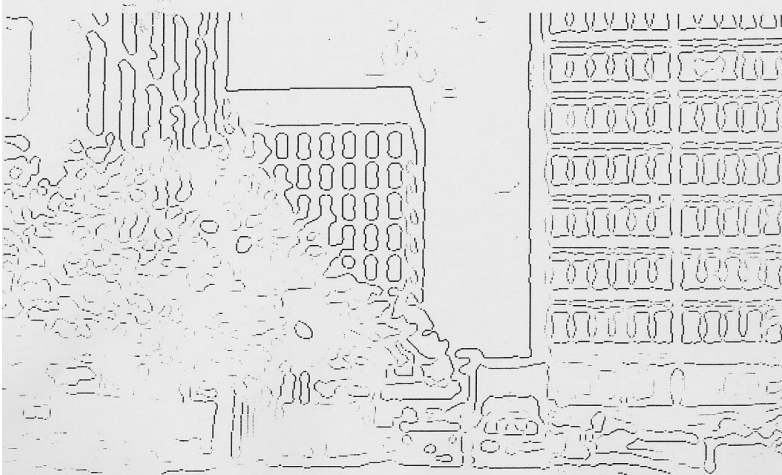
John Canny, Rachid Deriche, etc operators



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DoG + Sobel



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DoG(2, 9)+Sobel



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DoG(1, 9)+Sobel



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Template Matching

- ❖ An alternative method for edge detection computes the closest (over all four/eight directions) approximations of $g(i,j)$ in every 3×3 neighborhood, to keep the one with maximum convolution value, provided it is large enough
- ❖ Even if the sum of the kernel parameter is null note that starting with grey level images in the range $0:255$ the final range is $-3825:+3825$ and $-1275:1275$ for Kirsh and compass operators respectively (the equivalent are $-255:255$, $-765:765$, $-871:871$, $-1020:1020$ for Roberts, Prewitt, isotropic and Sobel respectively)
- ❖ Obviously the greater is the number of values different from zero of the kernel parameters the higher is the robustness to noise.



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Template Matching

❖ Kirsh's operator

-3-35	-355	555	55-3
-305	-305	-30-3	50-3
-3-35	-3-3-3	-3-3-3	-3-3-3
5-3-3	-3-3-3	-3-3-3	-3-3-3
50-3	50-3	-30-3	-305
5-3-3	55-3	555	-355

❖ Compass operator

-111	111	111	111
-1-21	-1-21	1-21	1-2-1
-111	-1-11	-1-1-1	1-1-1
11-1	1-1-1	-1-1-1	-1-11
1-2-1	1-2-1	1-21	-1-21
11-1	111	111	111

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3/9 operator

1 1 1	1 1 0	1 0 0	0 0 0
0 0 0	1 0 0	1 0 0	1 0 0
0 0 0	0 0 0	1 0 0	1 1 0
0 0 0	0 0 0	0 0 1	0 1 1
0 0 0	0 0 1	0 0 1	0 0 1
1 1 1	0 1 1	0 0 1	0 0 0

$$P_i = \sum_{j=0}^8 I_{i,j}$$

3	2	1
4	8	0
5	6	7

$$P_{i,j} = I_{i,j} + I_{i,j-1} + I_{i,j+1}$$

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Contour extraction

$$P=1.5 \left[\frac{P_{i,k}}{P_i} - 0.333 \right]$$

- ❖ $P_{i,k}$ is the maximum among the 8 parameters $P_{i,j}$
- ❖ The coefficients 3/2 et 1/3 are introduced to normalize the result
- ❖ The final threshold can be applied depending on the minimum average contrast τ admitted in the neighborhood

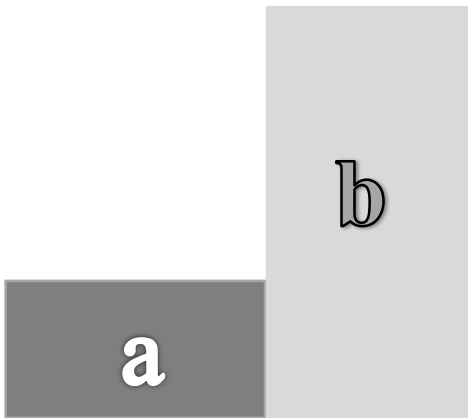
Practical aspects of the 3/9 filter

- ❖ The filter implements a relative gray level intensity analysis. Also the human eye apply a similar approach.
- ❖ It must be payed attention when looking contours in the dark!
- ❖ Note that if P_i is low this edge estimation suffers very much for the effect of the noise (if it is 0 the edge value determined by the ratio 0/0!).
- ❖ Selecting the threshold for P_i note that it is 9 time d_i average intensity of the area (if this intensity is 10 - over 255 – so very low P_i is 90: edges are looked for in the very dark)

Contrast and threshold

- ❖ Let us call 'contrast' the ratio $\tau = \frac{a}{b}$, the threshold Th is given by:

$$P_i = \frac{3}{2} \left[\frac{3b}{6a + 3b} - \frac{1}{3} \right]$$

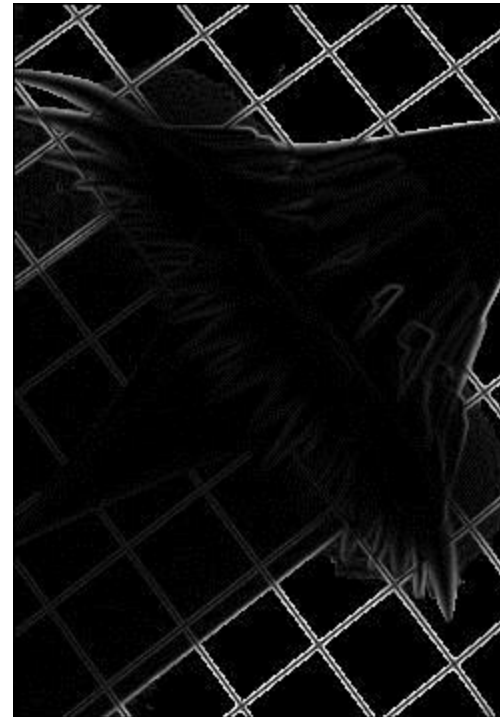
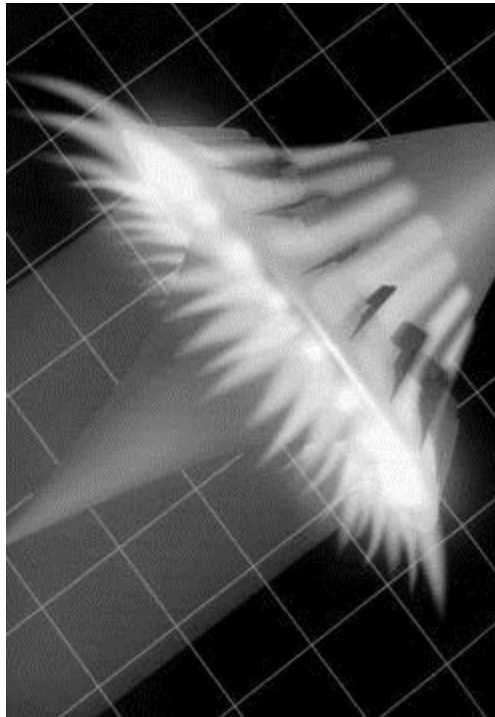


$$P_i = \frac{3}{2} \left[\frac{1}{2\tau + 1} - \frac{1}{3} \right]$$

$$Th = \frac{1 - \tau}{2\tau + 1}$$

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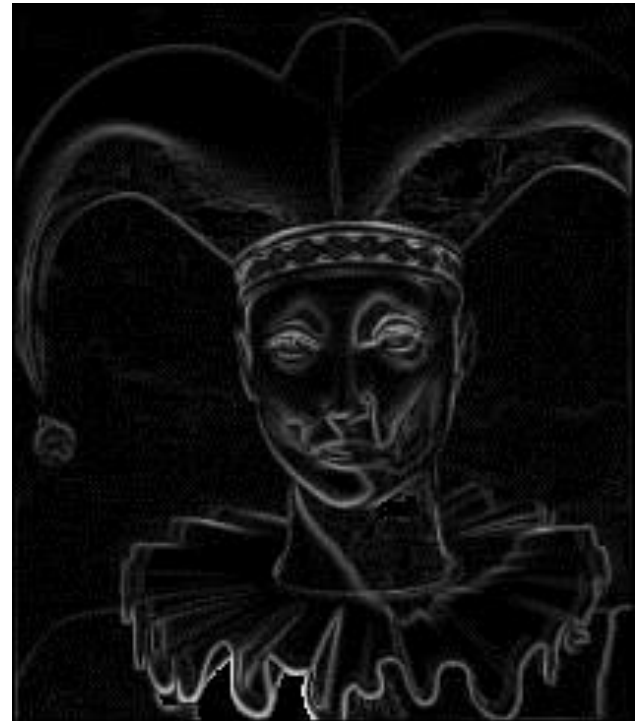
Example: Op. 3 / 9



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Example: Op. 3 / 9



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Degraded image: uniform noise

- ❖ The standard model of this noise is additive, independent at each pixel and independent of the signal intensity with continuous uniform distribution in a given interval. The noise caused by quantizing the pixels to discrete levels has an approximately uniform distribution.



This noise can be simulated adding in each pixel $N(i,j) = 2K(rnd - 0,5)$ being K the noise intensity and rnd a random number with $0 \leq rnd \leq 1$

Degraded image: ‘salt and pepper’

- ❖ This is an impulsive or spike noise for which the image has dark pixels and bright pixels randomly distributed.



This noise can be simulated for each pixel in this way:

if $rnd \geq Th_1$ $I(i,j) = 255$

if $rnd \leq Th_2$ $I(i,j) = 0$

else $N(i,j) = 2K(rnd - 0,5[1 - th_1 + th_2])$ and if $N(i,j) > 255$: $N(i,j) = 255$, if $N(i,j) < 0$: $N(i,j) = 0$
being K the uniform component noise intensity, $0 \leq rnd \leq 1$, and Th_1 and Th_2 two suitable thresholds ($1 - Th_1$ and Th_2 are the percentage of extra white and black pixels respectively)

Average value filter

❖ Each pixel takes the average value over the neighbors (3x3 in the example)

❖ Example - given the neighborhood:

	3	6	8
	3	4	2
	5	8	3

the central pixel will take the new value:

$$(3+6+8+3+4+2+5+8+3)/9 = 4.67$$

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Average value filter: uniform noise



Noisy image



Filtered image



Second iteration



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Average value filter: uniform noise



Noisy image



Filtered image



Second iteration

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Average value filter: salt and pepper



Noisy image



Filtered image



Second iteration

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Average value filter: salt and pepper



Noisy image



Filtered image



Second iteration

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Median and rank filters

- ❖ The median filter assigns to pixel the median value of neighborhood
- ❖ It is a particular case of the *rank filters* family, in which to the pixel is assigned the average value over a predefined range of the neighbors histogram.
- ❖ The average excluding the extremes is suited for impulse or spike noise such as the salt and pepper case.

- ❖ Example - given the neighborhood:

	3	6	8
	3	4	2
	5	8	3

the correspondent values are:

2	3	3	3	4	5	6	8	8
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median value: 4;
over three values: 4;
over five values: 4,2;
over seven values: 4,57
over nine values: 4,66

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Median filter: uniform noise



Noisy image

Filtered image

Second iteration

Rank 3

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Median filter: uniform noise



Noisy image



Filtered image



Second iteration



Rank 3

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Median filter: salt and pepper



Noisy image

Filtered image

Second iteration

Rank 3

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Median filter: salt and pepper



Noisy image



Filtered image



Second iteration



Rank 3

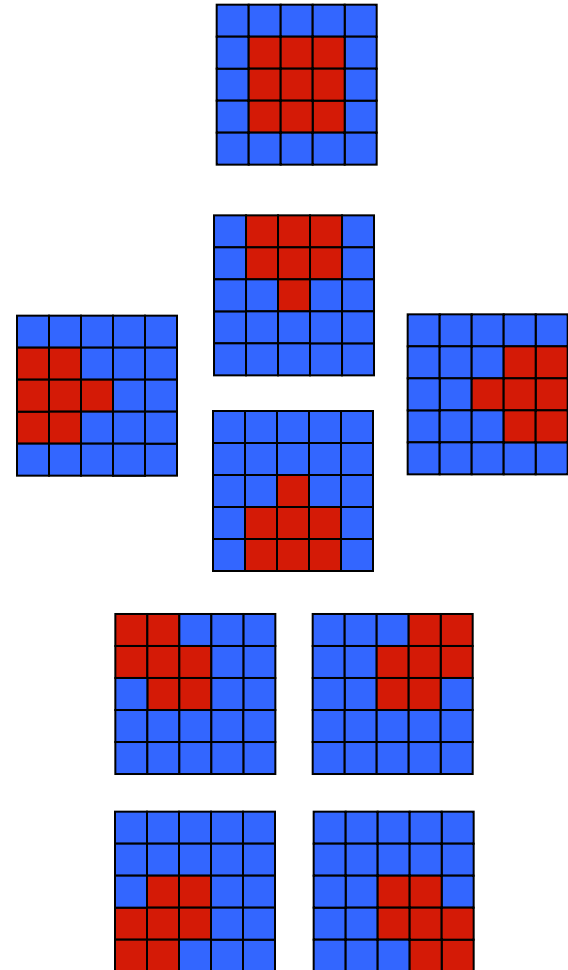
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The Nagao-Matsuyama Filter

This filter selects for the centre pixel the average for the orientation with the least variation. Hence, the steps are as follows:

1. Calculate the variance for each of the nine sub-groups shown to the right (including the centre pixel).
2. Determine the sub-group with the lowest variance.
3. Assign the mean of this sub-group to the centre pixel.



Nagao-Matsuyama improves the borders, and is effective at reducing the edges smoothing. Clearly there is a cost in terms of computation due to the calculation of nine variances for each pixel.

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Nagao filter: uniform noise



Noisy image



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Nagao filter: uniform noise



Noisy image



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Nagao filter: salt and pepper



Noisy image



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Nagao filter: salt and pepper



Noisy image



Filtered image

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Examples



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Examples

