

# Adaptive and Compressive Target Tracking Based on Feature Point Matching

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**Abstract**—In compressive tracking algorithms, a feature reduction projection matrix is constructed by using compressed sensing theory. Target and non-target objects are discriminated by using a naive Bayesian classifier. Such an algorithm may ensure accuracy of target tracking in real-time. But it is not adaptive for tracking with respect to scales and rotations. In this paper, we propose a novel adaptive algorithm based on feature point matching for tracking objects which appear with various changes. We combine weight-average and improved compressive tracking algorithms together for tracking objects, then calculate the corresponding feature points between two subsequent frames of the same object for obtaining the target changes related to various scales and rotations. Our experimental results show that the improved algorithm effectively improves the accuracy of target tracking and ensures adaptability of the tracking algorithm.

## I. INTRODUCTION

Target tracking technologies have manifold applications, for example in intelligent video surveillance, traffic systems, or mobile robotics. They are mainly employed to locate and understand targets of interest in video data for quantitative analysis. Object tracking is a fundamental step of target analysis. In the past decades, object tracking has been an extremely important research topic; for example, see [1]–[3] in computer vision.

Over years, significant progress has been achieved in target tracking. For instance, meanshift [4] has been typically applied to object tracking: the kernel density of a reference model and a candidate model (in a specific feature space) are employed, and matching scores of reference model and candidate model are compared. That candidate model with the maximum matching score was identified with the final position of the target.

Because the meanshift algorithm is not adaptive to scale changes of the target, Bradski [5] proposed the camshift algorithm, Zhang [7] presented a fast object tracking algorithm with *spatio-temporal context* [6] (STC) which extracted a model of the target position and its regional context based on Bayesian theorem according to the statistical correlation between the target and its context. Additionally it applied a confidence map to determine the final position of the target.

A tracking algorithm based on consistency of feature point matching is proposed in [8] which can process hundreds of frames per second. It combines pyramidal optical flow tracking

and feature point matching to determine the position of the target preliminarily, and then assigns to each feature point a vote. Those feature points which satisfy the consistency using a clustering algorithm are selected as the target position.

A kernel-related filter [10] leads to a fast object tracking algorithm; it is based on target detection [9] which extracts features of positive and negative samples by the circular shift method, and combines those by using the fast Fourier transform for training the classifier (for locating a target).

In recent deep learning, *Convolutional Neural Networks* (CNNs) achieve remarkable results for target tracking [11]–[13]. Due to the high computational complexity of neural networks, there are still real-time issues for these algorithms to be resolved.

Kalal [14] proposed a *long-term stable tracking* (TLD) algorithm which combined tracker and detector effectively. A compressive tracking algorithm [15] selects a proper feature space to establish a target model, and then constructs a classifier to discriminate the target and the background. This method combines generative models and discriminative models together effectively [16], [17].

Original compressive tracking cannot deal with changes in scale and rotation. For solving this problem, there are various improvements [18]–[20]. For example, Zhang [18] uses structure constraints for the target to ensure multiscale samples. In [19], Affine transforms of samples were adopted to obtain different scales and rotations.

Different to existing work, in order to achieve the real-time effect (i.e. to reduce the computational complexity), in this paper we use feature points to obtain scaling and rotation factors of tracking targets. To the best of our knowledge, this is the first time to improve the adaptability of a compressive target tracking algorithm. We implemented the improved algorithm and report our promising experimental results.

The paper is structured as follows. Section II outlines compressive tracking. Section III provides our novel additions to the approach. Our work in this paper is discussed in Section IV. Section V concludes.

## II. COMPRESSIVE TRACKING

### A. Feature Extraction

Feature extraction requires convolutions using multiscale rectangular filters designed by using positive and negative

samples. Based on the convolutions, we obtain feature vectors of different lengths. These vectors are concatenated to form a high-dimensional vector, named as the *vector of a multiscale rectangular feature*. For a sample:  $\mathbf{z} \in \mathbb{R}^{w \times h}$  the multiscale rectangular filter is a set of functions  $\{h_{1,1}, h_{1,2}, \dots, h_{w,h}\}$ , defined as

$$h_{i,j}(x, y) = \begin{cases} 1 & \text{if } 1 \leq x \leq i \text{ and } 1 \leq y \leq j \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

where  $0 < i \leq w$  and  $0 < j \leq h$  represent the width and height of the rectangular filter, respectively, and  $x$  and  $y$  are the pixel coordinates in a multiscale rectangular filter. Then, we represent each filtered image as a column vector  $\mathbf{X}$  in a very high-dimensional image space  $\mathbb{R}^m$ . The dimensionality  $m$  is typically in the order of  $10^6$  to  $10^{10}$ .

In order to ensure real-time tracking, compressive sensing theory [21] was used to reduce the dimension of the image vectors  $\mathbf{X}$ . The compressive sensing theory [21] analyses mappings of signals  $\mathbf{X}$  by a special projection matrix  $\mathbf{P}$  for redundancy reduction. The result  $\mathbf{V} = \mathbf{P}\mathbf{X}$  maps a high-dimensional vector from image space into a low-dimensional (say,  $n$ -dimensional) space of feature vectors, with assuming that  $n \ll m$ . The original signal  $\mathbf{X}$  can be reconstructed from  $\mathbf{V}$  with very high probability [22].

The random projection matrix  $\mathbf{P} = [p_{i,j}]$  is as follows:

$$p_{i,j} = \sqrt{s} \times \begin{cases} 1 & \text{with probability } \frac{1}{2s} \\ 0 & \text{with probability } 1 - \frac{1}{s} \\ -1 & \text{with probability } \frac{1}{2s} \end{cases} \quad (2)$$

where  $s$  is often recommended to be equal to 2 or 3. The matrix  $\mathbf{P}$  is very sparse and satisfies the *restricted isometry property* (RIP). The literature also discusses  $s = m/4$  which means that we only have four non-zero numbers at most in the projection matrix  $\mathbf{P}$ ; thus this greatly reduces the computational complexity.

### B. Design of the Classifier

Compressive target tracking adopts a naive Bayesian classifier which is based on the assumption that elements of the feature vector are independent on the sense of a normal distribution. The specific classifier is modeled in [14] as follows:

$$\begin{aligned} H(V) &= \log\left(\frac{\prod_{i=1}^n p(v_i|y=1)p(y=1)}{\prod_{i=1}^n p(v_i|y=0)p(y=0)}\right) \\ &= \sum_{i=1}^n \log\left(\frac{p(v_i|y=1)}{p(v_i|y=0)}\right) \end{aligned} \quad (3)$$

where  $y$  represents a sample label, and  $p(y=1) = p(y=0) = 0.5$  are the prior probabilities of positive and negative sample, respectively.  $v_i$  represents the  $i$ -th detected sample feature, then the current target position was the sample with the biggest  $H(V)$ .

The random projection of a high-dimensional random vector almost satisfies a Gaussian distribution  $p(v_i|y=1) \sim$

$N(\mu_i^1, \delta_i^1)$ ,  $p(v_i|y=0) \sim N(\mu_i^0, \delta_i^0)$ . Therefore, the conditional probability of the positive and negative samples is also consistent with the Gaussian distribution. The parameters of these Gaussian distributions are constantly updated as follows:

$$\begin{aligned} \mu_i^1 &= \lambda\mu_i^1 + (1-\lambda)\mu^1 \\ \delta_i^1 &= \sqrt{\lambda(\delta_i^1)^2 + (1-\lambda)(\delta^1)^2 + \lambda(1-\lambda)(\mu_i^1 - \mu^1)^2} \end{aligned} \quad (4)$$

where  $\mu^1$  and  $\delta^1$  represent mean and variance of the dimension-reduced feature vectors of the  $i$ -th sample, respectively, and  $\lambda$  is a learning factor.  $\mu_i^1$  and  $\delta_i^1$  are the updated mean and variance.

Finally, that object region (of rectangular shape) having the biggest classification score is the detected position of the target.

### III. SCALE AND ROTATION-BASED ADAPTIVE COMPRESSIVE TRACKING

The common sampling method of compressive tracking is presented in the following equations:

$$R_p = \{\gamma_{1p} \leq \|R_p - R_{t-1}\| < \gamma_{2p}\} \quad (5)$$

$$R_n = \{\|R_n - R_{t-1}\| > \gamma_n\} \quad (6)$$

$$R_d = \{\|R_d - R_{t-1}\| < \gamma_d\} \quad (7)$$

where  $R_p$ ,  $R_n$ , and  $R_d$  represent the sets of positive samples, negative samples, and detected samples, respectively.  $\gamma_{1p}$ ,  $\gamma_{2p}$ ,  $\gamma_n$ , and  $\gamma_d$  are thresholds for sample collection given based on observations.  $R_{t-1}$  is the target position of last frame, we can see that all samples can be obtained based on it. The collected samples have only slight changes related to locations; the sample sizes are always identical. Therefore, compressive tracking cannot track targets with scale or rotation changes.

In compressive target tracking, drift errors are usually occurring in cases of intense movement, occlusion, or similarity in color or silhouettes (i.e. appearance). In compressive tracking, selecting the sample having the highest score as the target location is improper sometimes, although the sample might be more similar to the target than others, least resembling to the shown background, the corresponding region of this sample cannot reflect the exact location of the target.

Therefore, in this paper we propose a target localization method based on averaging weighted multi-rectangles [23]. We compute the average of weights as the scores. We regard the weighted average of the top  $N > 0$  rectangular regions  $G_i$  as the candidate for the target location:

$$G_o = \frac{1}{N} \sum_{i=1}^N \omega_i \cdot G_i \quad (8)$$

where  $G_o$  is the final target position, and  $G_i$  is the location of the  $i$ -th sample amongst all the selected samples;  $\omega_i$  represents the weight of the  $i$ -th sample.  $\omega_i$  is defined as follows:

$$\omega_i = \begin{cases} \frac{H(V_{G_i})}{H(V)} & H(V_{G_i}) > \overline{H(V)} \\ \frac{H(V)}{H(V_{G_i})} & H(V_{G_i}) < \overline{H(V)} \end{cases} \quad (9)$$

where  $\overline{H(V)}$  is the average score of the top  $N$  rectangular regions,  $H(V_{G_i})$  represents the  $i$ th detected sample score.

Applying this method we are not only able to deal with a range of target scale changes in target tracking, we are also able to better exclude the interference by similar objects. We show that this approach offers the possibility of improving the accuracy of object tracking.

We also propose an adaptive compressive tracking algorithm based on feature-point matching. The original algorithm flowchart is shown in Fig. 1.

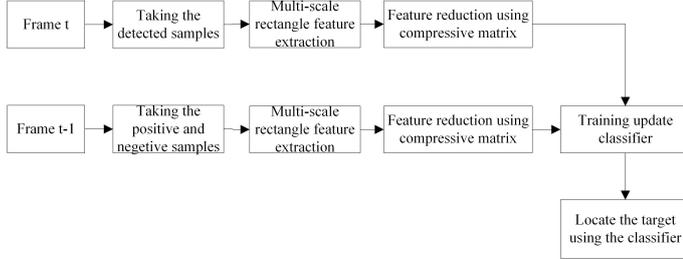


Fig. 1. Flowchart of our compressive tracking

Figure 1 is the flowchart for the initial phase of compressive tracking. According to the position in frame  $t - 1$ , we first collect the positive and negative samples using Eqs. (5) and (6). Then we compute the multiscale rectangular features of the collected samples and reduce the feature dimensions so as to train the classifier. We take the detected samples and the reduced feature vector for frame  $t$  in the same way as for frame  $t - 1$ . Finally, we get scores in frame  $t$  by using the classifier trained by frame  $t - 1$  to classify the detected samples. The final location of the target is the weighted average of the top  $N$  regions  $G_i$  where the corresponding classification scores are ranked.

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#### Algorithm 1 Compute scale and rotation factor

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**Input:**  $frame_t, frame_{t-1}, Rect_t, Rect_{t-1}$

**Output:**  $\alpha, \theta$

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1: function GETFACTOR( $frame_t, frame_{t-1}, Rect_t, Rect_{t-1}$ )
2:    $ROI_t \leftarrow SetROI(frame_t, Rect_t)$ ,
3:    $ROI_{t-1} \leftarrow SetROI(frame_{t-1}, Rect_{t-1})$ 
4:    $KP_t \leftarrow detect(ROI_t)$ 
5:    $KP_{t-1} \leftarrow detect(ROI_{t-1})$ 
6:    $M \leftarrow match(KP_t, KP_{t-1})$ 
7:    $num\_point \leftarrow estimate\_num()$ 
8:   if  $num\_point > T$  then
9:      $\alpha \leftarrow estimate\_scale(M_t, M_{t-1})$ 
10:     $\theta \leftarrow estimate\_rotation(M_t, M_{t-1})$ 
11:   else
12:     Return to detect the target
13:   end if
14: end function
  
```

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#### A. Scale-based Adaptive Target Tracking

We illustrates how to calculate the object scaling and rotation factor in Algorithm 1. We first detect feature points

[24], [25] of the target position in frames  $t$  and  $t - 1$ , respectively, and match those based on the Euclidean distance [26]. Finally we obtain the scaling factors based on the successfully matched feature points in the considered adjacent frames.

At the same time, we use a trained threshold to ensure a high tracking accuracy rate. If the number of successfully matched points is bigger than the threshold, the tracking result is positive, otherwise we need to relocate the object.

During the process, the feature points of the ROI region are modeled as follows:

$$KP = \{(p_i, d_i) | 0 < i \leq num\_point\} \quad (10)$$

where  $p_i$  represents the point plane coordinate,  $d_i$  is the descriptor of the feature. Then Euclidean distance is used for descriptors matching:

$$d(d_i, d_j) = \|d_i - d_j\| \quad (11)$$

The computation of a scaling factor is given by the following equation:

$$\alpha_{i,j} = \frac{d_{i,j}^t}{d_{i,j}^{t-1}} = \frac{\|p_i^t - p_j^t\|}{\|p_i^{t-1} - p_j^{t-1}\|} \quad (12)$$

where  $d_{i,j}^t$  represents the Euclidean distance between pixels  $p_i^t$  and  $p_j^t$  in frame  $t$ .

In the same way,  $d_{i,j}^{t-1}$  is the Euclidean distance between pixels  $p_i^{t-1}$  and  $p_j^{t-1}$  in frame  $t - 1$ .  $p_i^{t-1}$  is the matching point to  $p_i^t$  in frame  $t - 1$ , so is  $p_j^t$  to  $p_j^{t-1}$ . We choose the mean or the median of those  $\alpha_{i,j}$  values as the final scaling factor  $\alpha$ .

#### B. Rotation-based Adaptive Target Tracking

The angle of rotation is computed as follows:

$$\theta_{i,j} = atan2(y_{i,j}^t, x_{i,j}^t) - atan2(y_{i,j}^{t-1}, x_{i,j}^{t-1}) \quad (13)$$

where  $y_{i,j}^t$  and  $y_{i,j}^{t-1}$  represent the distance between pixel  $i$  and pixel  $j$  in  $y$ -direction in frame  $t$  and  $t - 1$ , respectively.  $x_{i,j}^t$  and  $x_{i,j}^{t-1}$  are the distances between pixels  $i$  and  $j$  in  $x$ -direction in frames  $t$  and  $t - 1$ , respectively. Again we choose either the median or the mean of the  $\theta_{i,j}$  values as the final scale factor  $\theta$ .

We obtain the 2-dimensional rotation matrix for angle  $\theta$ :

$$\mathbf{R} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \quad (14)$$

Therefore, the final target position is expressed as follows:

$$G_{tf} = \alpha \cdot \mathbf{R} \cdot G_t \quad (15)$$

where  $G_{tf}$  is the final object position;  $G_t$  represents the position prior to scaling and rotation.

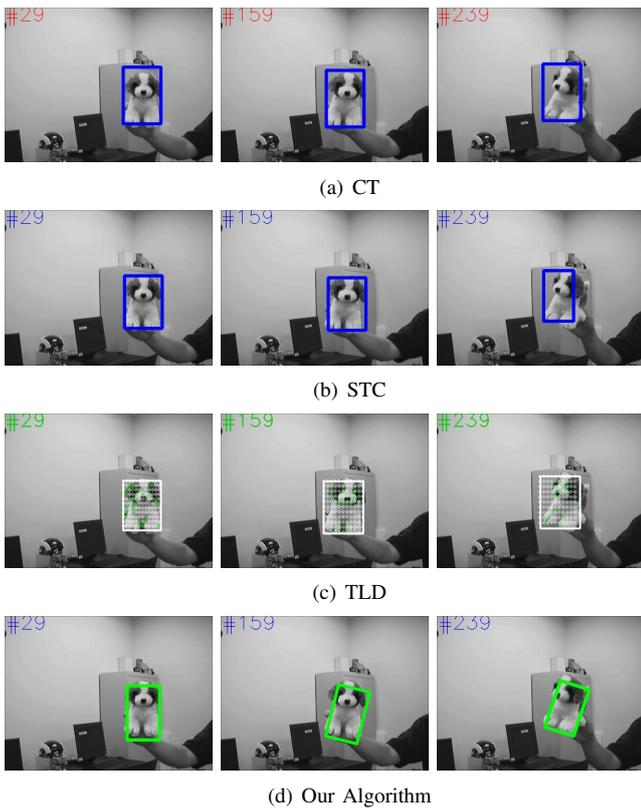


Fig. 2. dog results

#### IV. EXPERIMENTAL RESULTS AND ANALYSIS

In this paper, we choose seven video sequences and four target tracking algorithms to verify the validity of the proposed algorithm. The video sequences are dog [6], juice [6], David [10], bike [10], dollar [10], toy [6], and mountain-bike [6]. The tracking algorithms are *compressive tracking* (CT), *spatio-temporal context tracking* (STC), *tracking learning detection* (TLD), and our tracking algorithm. The tracking results are shown from Fig. 2 to Fig. 8.

For the experiment with object *dog*, these four tracking algorithms all track the target successfully, but only the proposed algorithm correctly reflects rotations of the target, as shown in Fig. 2(d). CT did not provide any indication of target scale and rotation, and STC and TLD were able to track the changes with respect to target scale, but not with respect to target rotation. STC depends on the context of objects severely, tracking errors happen at the edge of the object. For example, we can find tracking drifts in frame 239 in Fig. 2(b).

For *juice*, the STC algorithm is the best both in tracking accuracy and for scaling. It has tracking errors due to the interference of similarity in TLD. Compared with original compressive tracking, our algorithm can track size changes, but there is some slight tracking drift.

Scaling changes for *David* are not significant, so all the methods can track the position of the target. Although there exists a drift in both CT and our method, but the drift is greatly reduced in our algorithm. This indicates that compressive

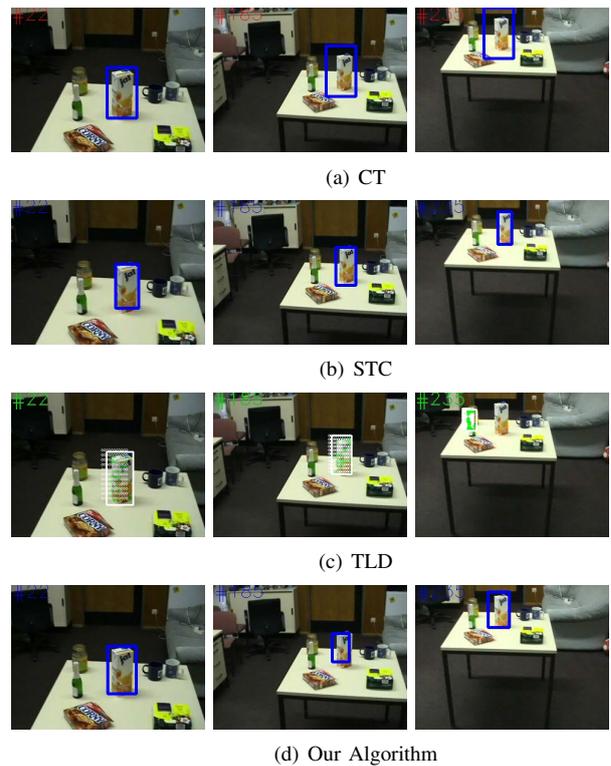


Fig. 3. juice results

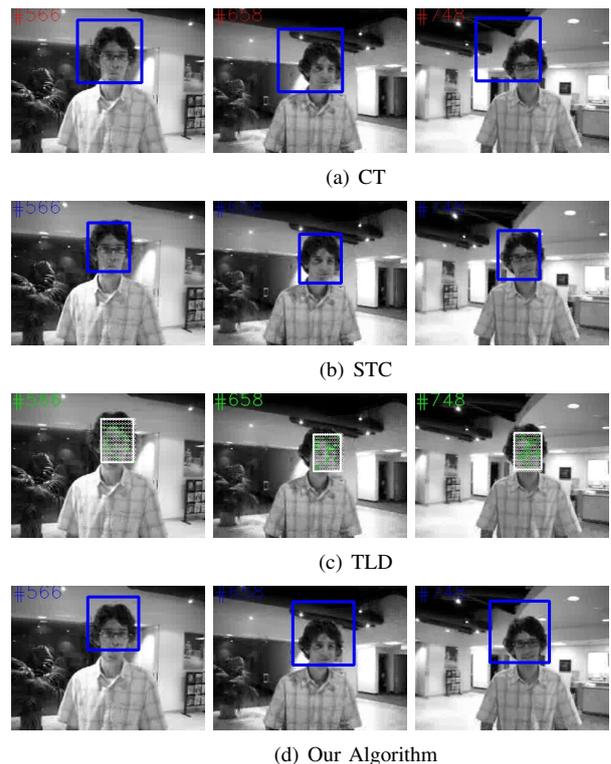


Fig. 4. David results

tracking is dependent on the choice of the initial position. The TLD tracking method, combined with target detection

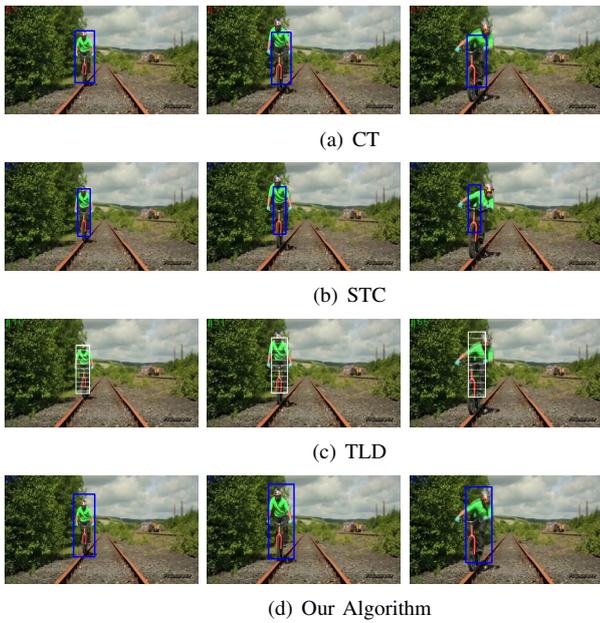


Fig. 5. bike results

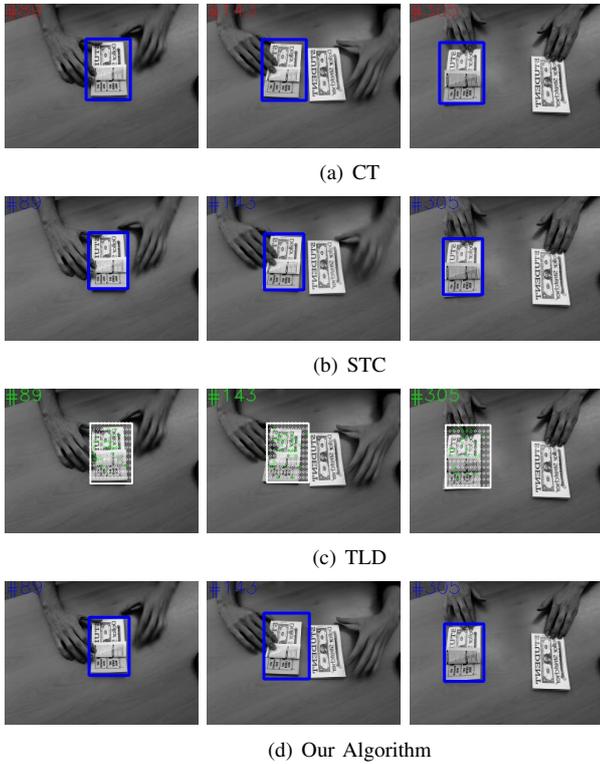


Fig. 6. dollar results

and model learning, has a reduced dependency on the initial position, and STC is much more stable and accurate in tracking compared to TLD.

For *bike*, compared with CT, our algorithm is much more robust. TLD and STC also process scaling changes, but it can be seen from frames 37 and 65 that the results of scale-based

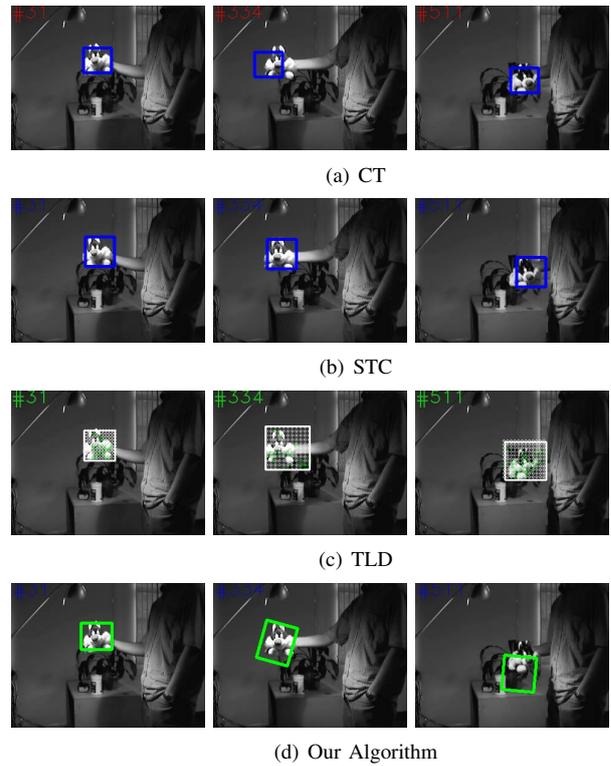


Fig. 7. toy results

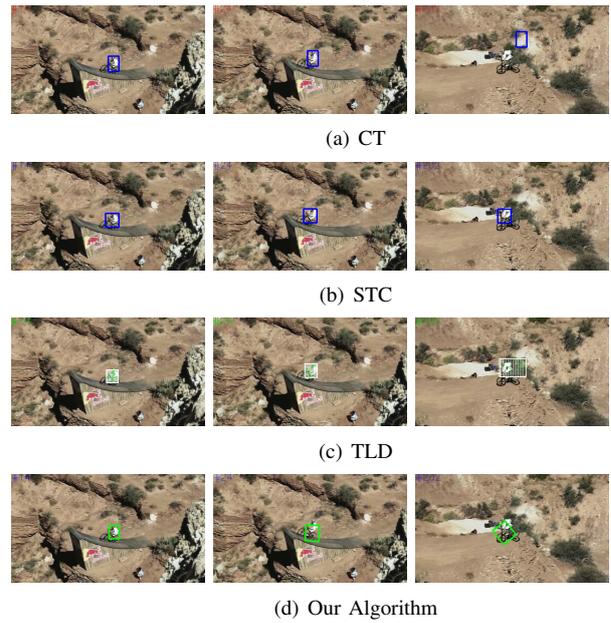


Fig. 8. mountain-bike results

adaptive tracking are not ideal, so these two algorithms still have room to be improved.

The four algorithms track the object *dollar* accurately. But, according to our observations, compressive tracking cannot locate the target correctly when the given initial position varies. This indicates that the initial target position plays a

pivotal role in compressive tracking. In our algorithm, the initial target position is given by a number of feature points, which greatly reduces the dependency on the initial position and increases the tracking success rate tremendously.

Figures 7 (toy) and 8 (mountain-bike) illustrate again rotation-adaptive test results for these two videos. The first column shows initial object positions. The other two columns show tracking results. It can be seen that our algorithm can deal with object rotation changes well for these two videos, in difference to the other three algorithms.

Tracking success rates of the compared four methods, for all the used video test data, are summarised in Table I.

TABLE I  
COMPARISON OF TRACKING SUCCESS RATES

Video	CT	STC	TLD	Ours
dog	93%	94%	96%	98%
juice	84%	91%	95%	88%
David	90%	93%	92%	93%
bike	73%	75%	85%	90%
dollar	69%	93%	90%	93%
toy	92%	94%	95%	96%
mountain-bike	86%	92%	96%	93%

The algorithm evaluation criteria is defined as:

$$VE = \sqrt{\sum_{i=1}^4 (p_i - p_g)^2} \quad (16)$$

if  $VE < \sqrt{w^2 + h^2}$ , it means tracking success.  $p_i$  is the plane coordinate of the rectangular's vertex,  $p_g$  indicates the ground truth of target position.

## V. CONCLUSIONS

The originally proposed compressive tracking algorithms have not the ability to track objects when changing scales or rotating. In order to overcome these drawbacks, we proposed adaptive compressive tracking based on feature point matching. We calculate the changes of scale and rotation by computing ratios and angles of matching feature points between subsequent frames. At the same time, we decide whether the number of successfully matching points satisfy the given thresholds or not, so as to relocate the target. Our experimental results show that the algorithm, proposed in this paper, effectively improves compressive target tracking, and also tracks targets showing changes with respect to scaling or rotation with improved accuracy.

## VI. ACKNOWLEDGMENTS

This project was supported by the Natural Science Foundation of Shandong Province China (No. ZR2014YL010), and the Shandong Science and Technology Development Program China (No. 2014GSF120018).

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